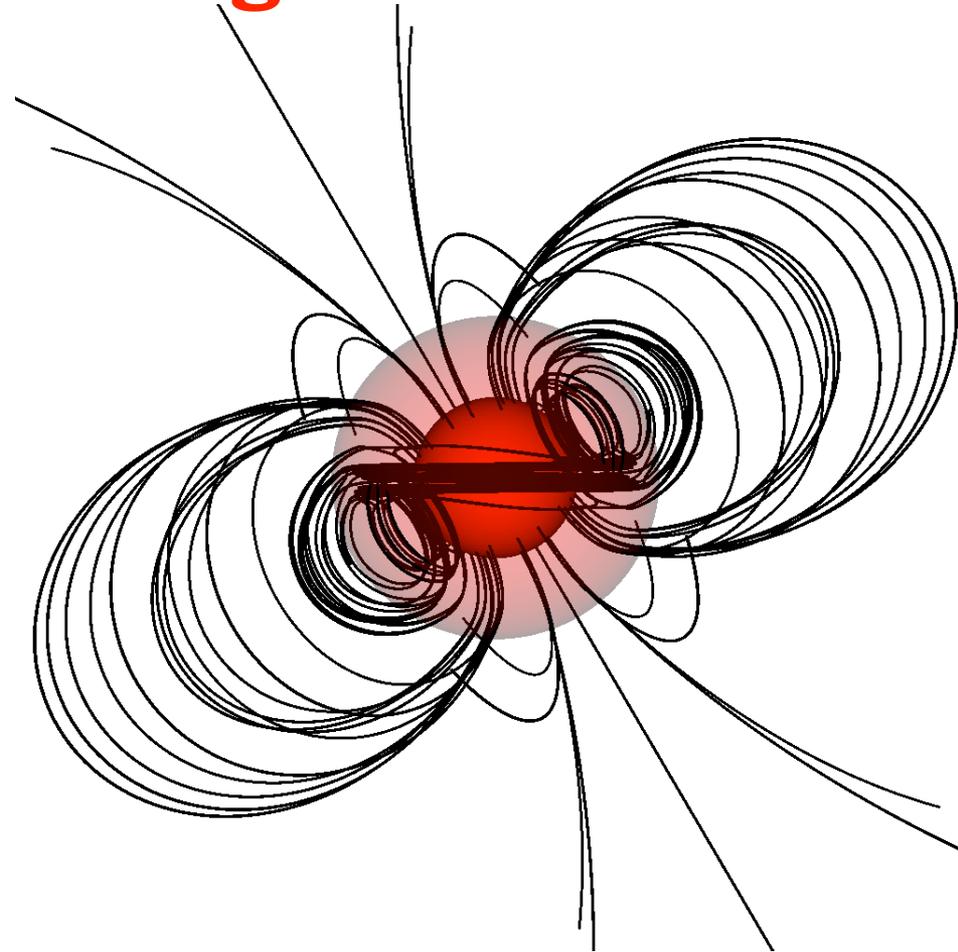


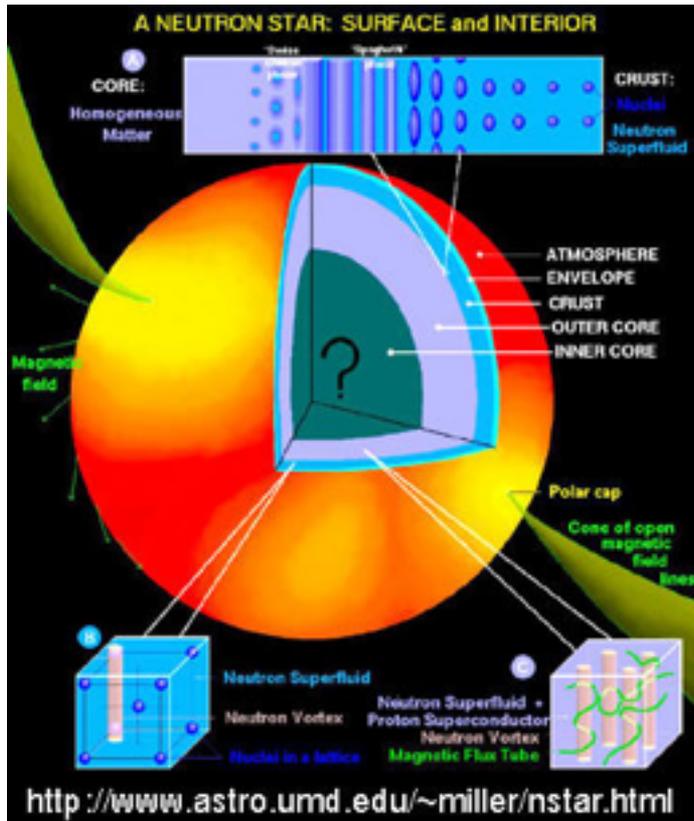
Determining observational properties of neutron stars by modelling their interiors

Paul Lasky

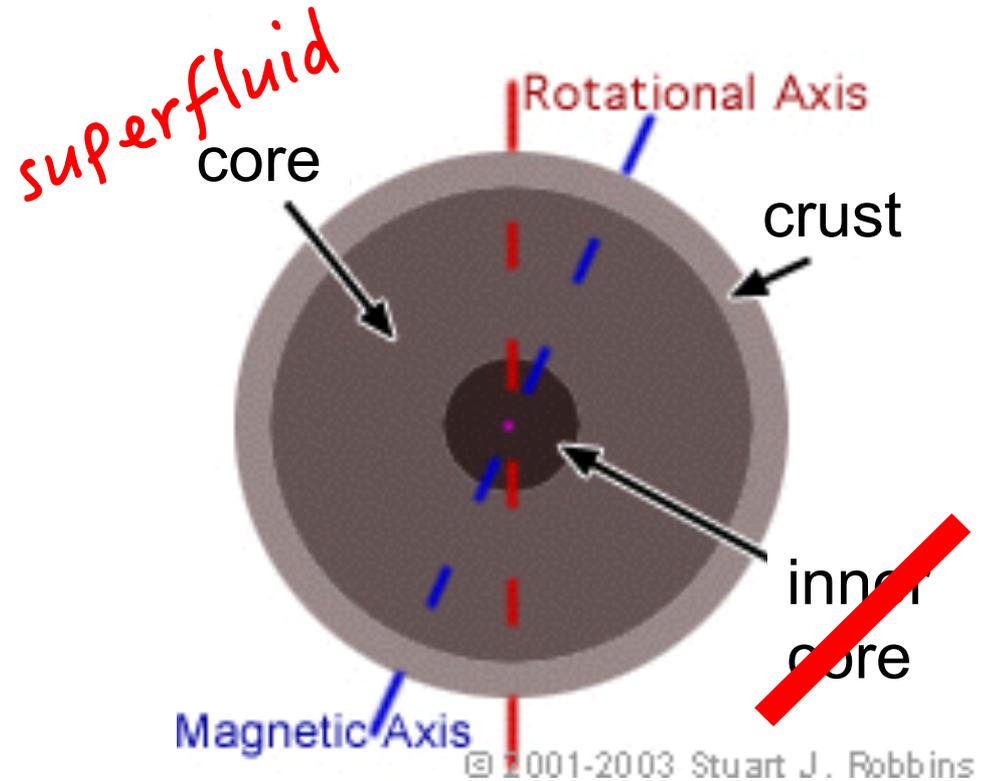


Neutron Star Anatomy

Fiducial neutron star talk



This neutron star talk

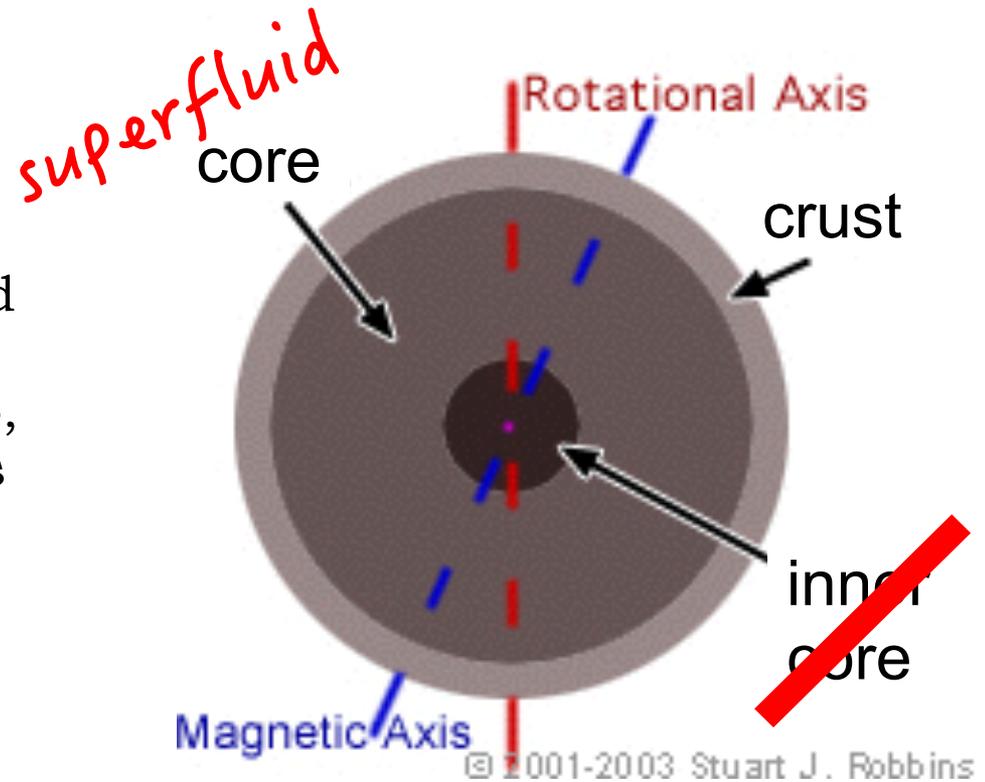


Neutron Star Anatomy

This neutron star talk

Greenstein
(1970; Nature)

Abstract: The neutron superfluid in most neutron stars should be in a highly turbulent state. If so, this turbulence drastically alters its rotational properties.



summary

**Crust & Core:
do they corotate? (no)**

**theoretical
implications**

A turbulent core?

**Magnetic fields in
the crust?**

**observational
implications**

**pulsar
timing
noise**

**gravitational
waves**

**magnetar
heating,
evolution &
flares**

The core and the crust

Conventional wisdom:

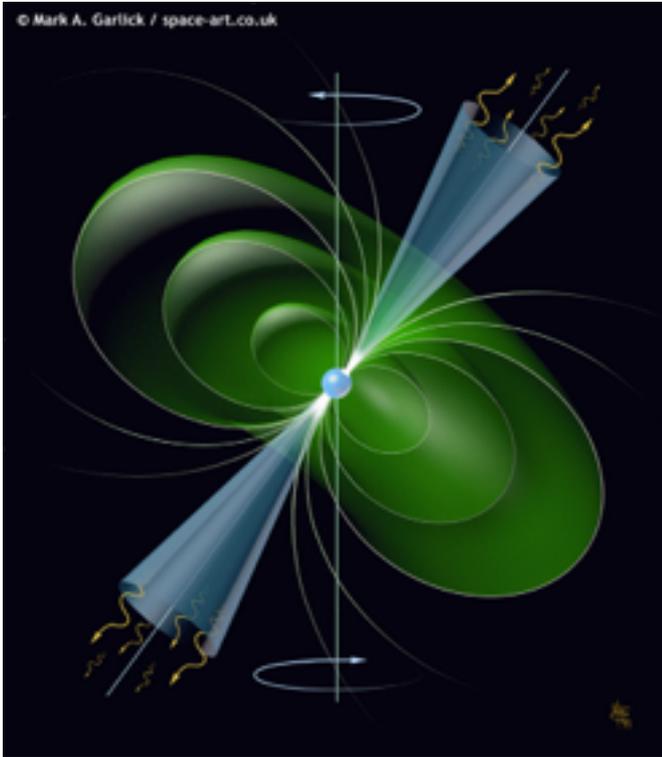
- Neutron star's crust & core *corotate*
- 2 mechanisms:
 - viscous coupling (Ekman pumping)
 - magnetic coupling (commonly considered dominant)

The conventional wisdom is wrong!

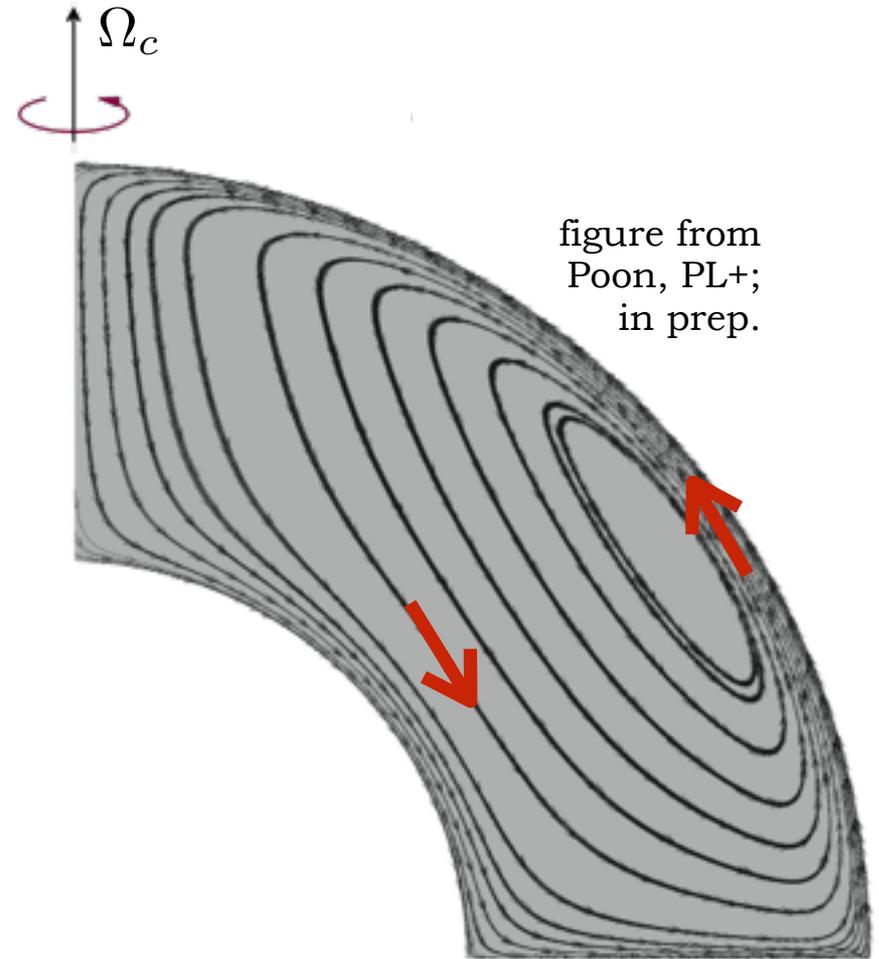
Neither mechanism can effectively enforce crust-core corotation (Melatos 2012; Glampedakis & PL 2015)

- Theoretical & Observational implications

Ekman pumping



**magnetic field
spins down crust**



**Ekman pumping spins
down fluid in core**

Ekman pumping



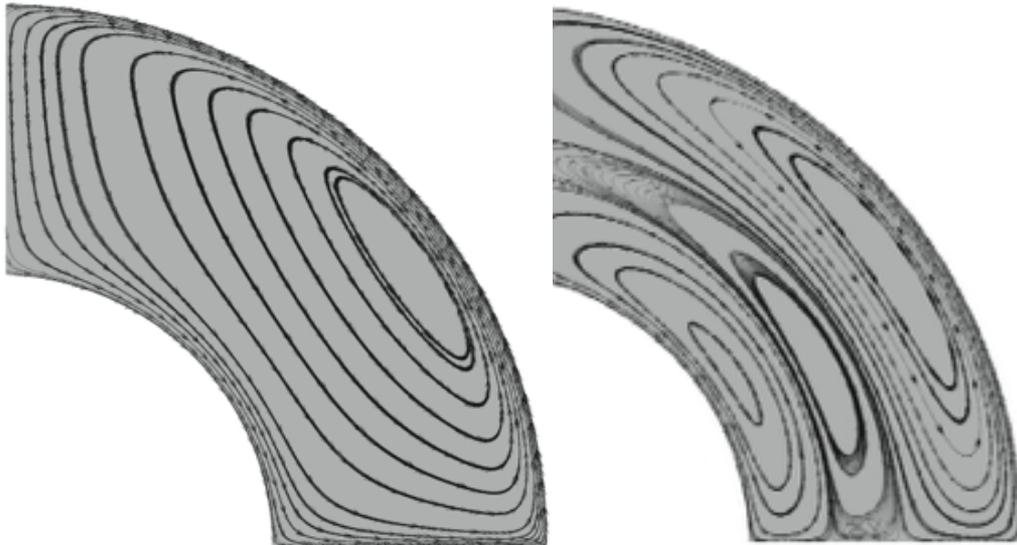
Vortex flow at the Canberra airport

*"this is something that only
physicists can get excited
about..."*

Alexander Heger

stratified Ekman pumping

- Ekman flow hindered by stratification (Abney & Epstein 1996)
- Only effective in thin layer near crust-core boundary
- Rest of core couples on much longer timescale ($\sim 10^3$ yr; Melatos 2012)



**Melatos 2012:
neutron stars have
super-rotating cores!**

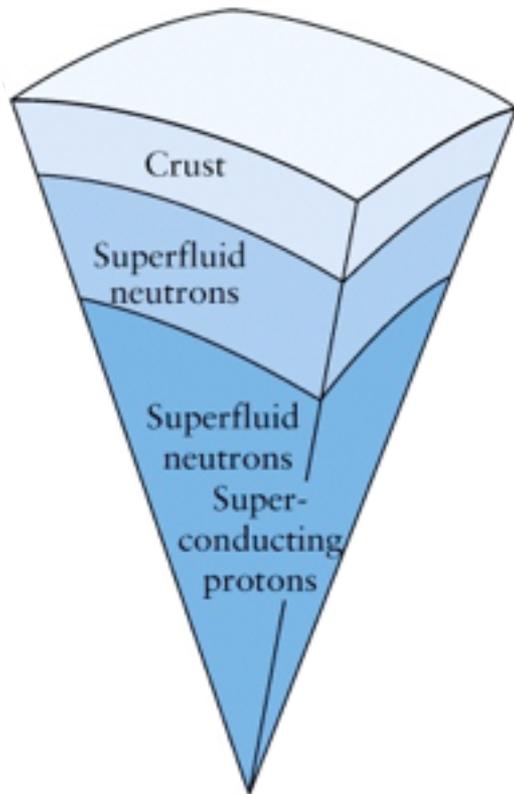
caveat:
the magnetic field!

magnetic crust-core coupling

Glampedakis & PL (2015)

Model

- Two-fluid core (charged proton-electron fluid + neutron superfluid) magnetically coupled to the crust.



<http://www.ualberta.ca/>

- in crust's instantaneous rest frame, the secular dynamics of charged component is

$$2\boldsymbol{\Omega} \times \mathbf{v}_p + \dot{\boldsymbol{\Omega}} \times \mathbf{r} + \nabla \Psi_p = \frac{1}{\rho_p} (\mathbf{F}_{\text{mag}} - \mathbf{F}_{\text{cpl}})$$
$$2\boldsymbol{\Omega} \times \mathbf{v}_n + \dot{\boldsymbol{\Omega}} \times \mathbf{r} + \nabla \Psi_n = \frac{1}{\rho_n} \mathbf{F}_{\text{cpl}}$$

Ψ : chemical + gravitational potentials

\mathbf{F}_{mag} : magnetic force

\mathbf{F}_{cpl} : coupling force with neutrons

magnetic crust-core coupling

Glampedakis & PL (2015)

The punch line

- Degree of coupling between the crust and the core depends sensitively on the magnetic field **geometry!**

magnetic crust-core coupling

Glampedakis & PL (2015)

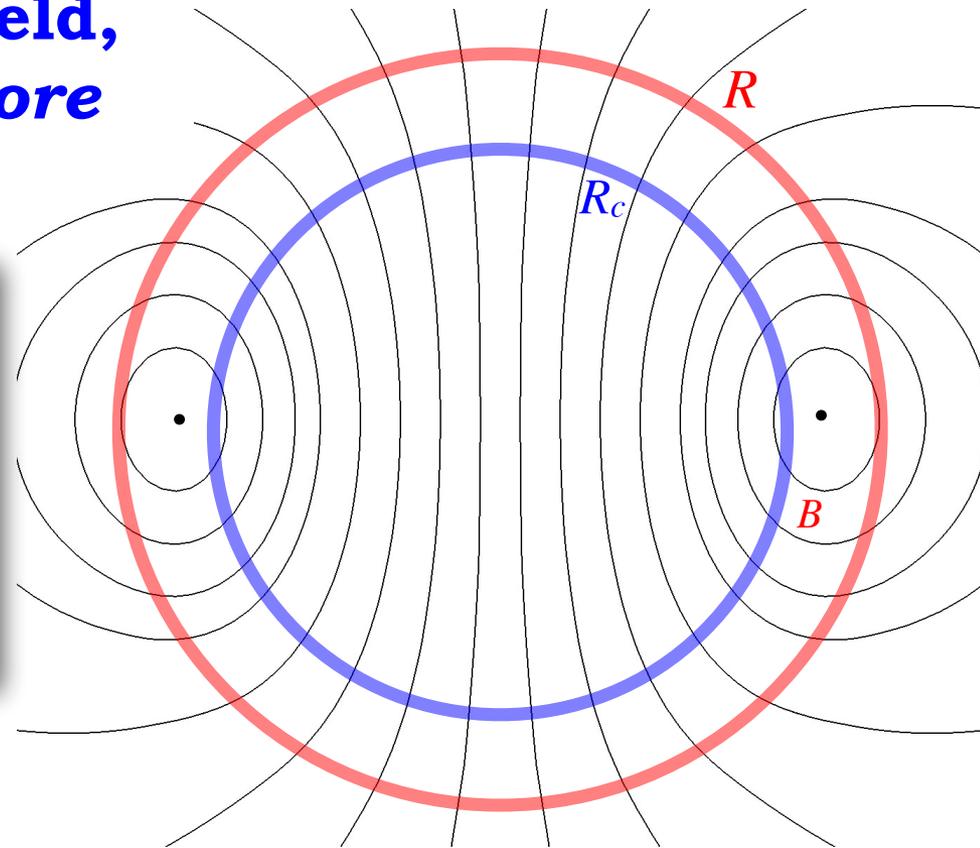
The punch line

- Degree of coupling between the crust and the core depends sensitively on the magnetic field **geometry!**

Case 1: purely poloidal field, *no closed field lines in core*

**Entire core couples to
crust and corotates.**

**Crust and core spin
down in unison**



magnetic crust-core coupling

Glampedakis & PL (2015)

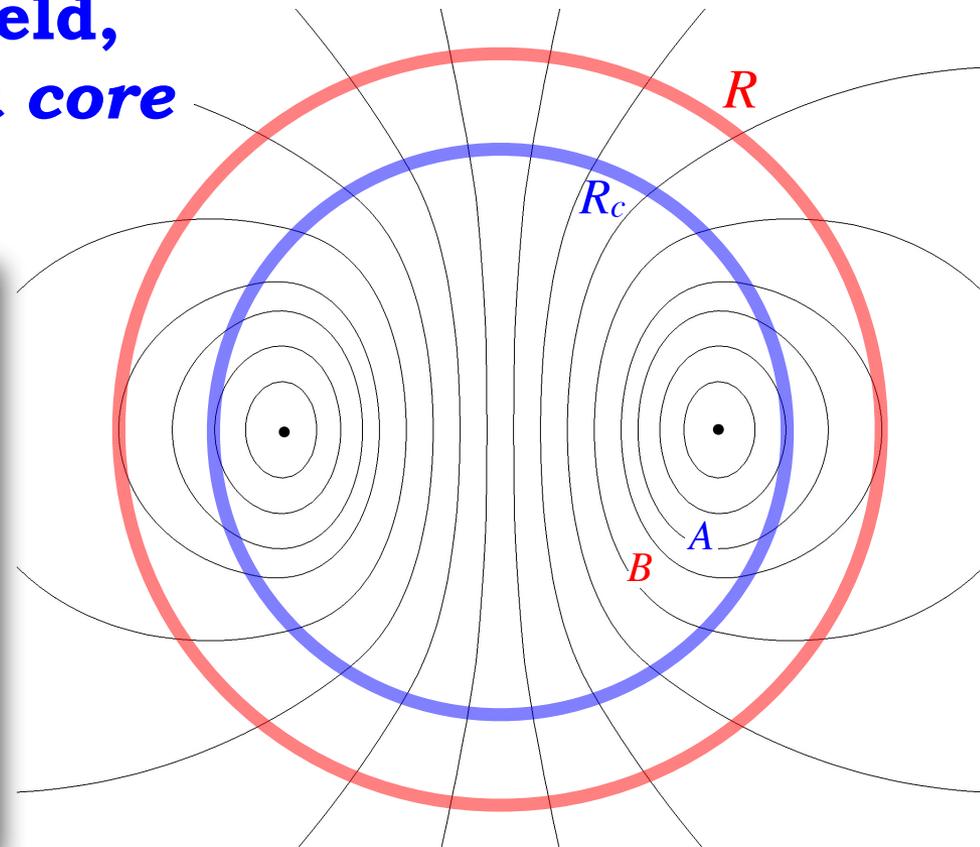
The punch line

- Degree of coupling between the crust and the core depends sensitively on the magnetic field **geometry!**

Case 2: purely poloidal field, with closed field lines in core

*Only core region
threaded by open field
lines corotates with
the crust*

**Rest of the core
is decoupled**



magnetic crust-core coupling

Glampedakis & PL (2015)

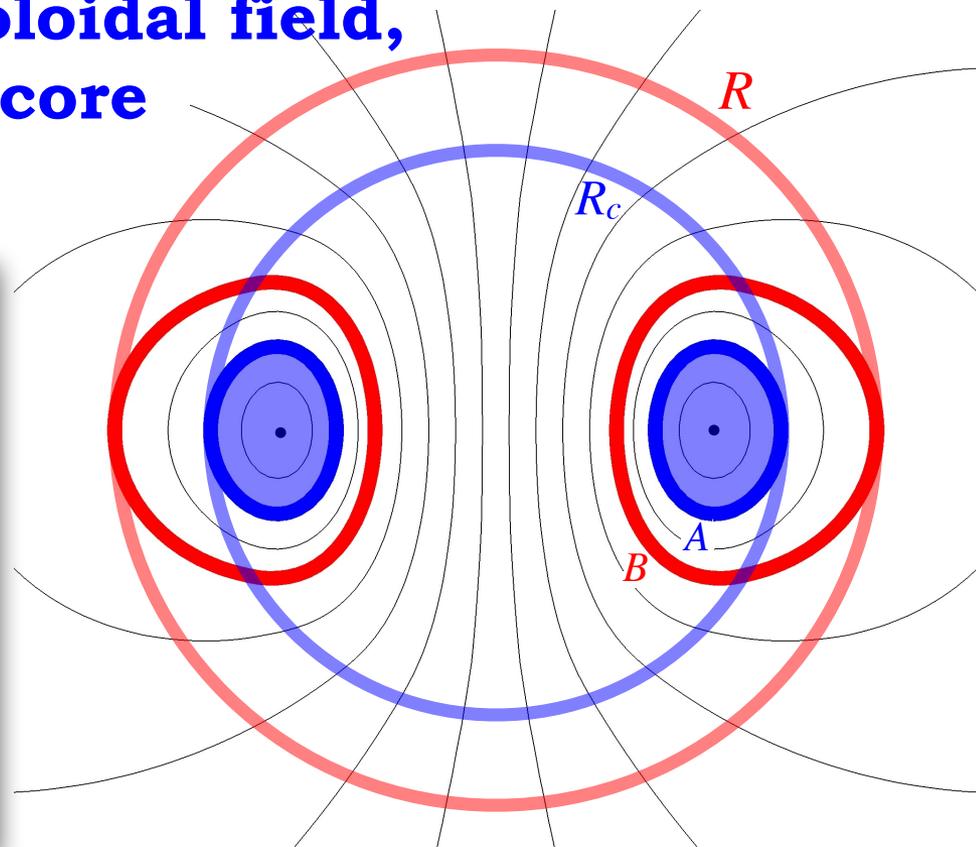
The punch line

- Degree of coupling between the crust and the core depends sensitively on the magnetic field **geometry!**

Case 3: mixed toroidal-poloidal field, with closed field lines in core

Only core region threaded by open field lines corotates with the crust

Rest of the core is decoupled

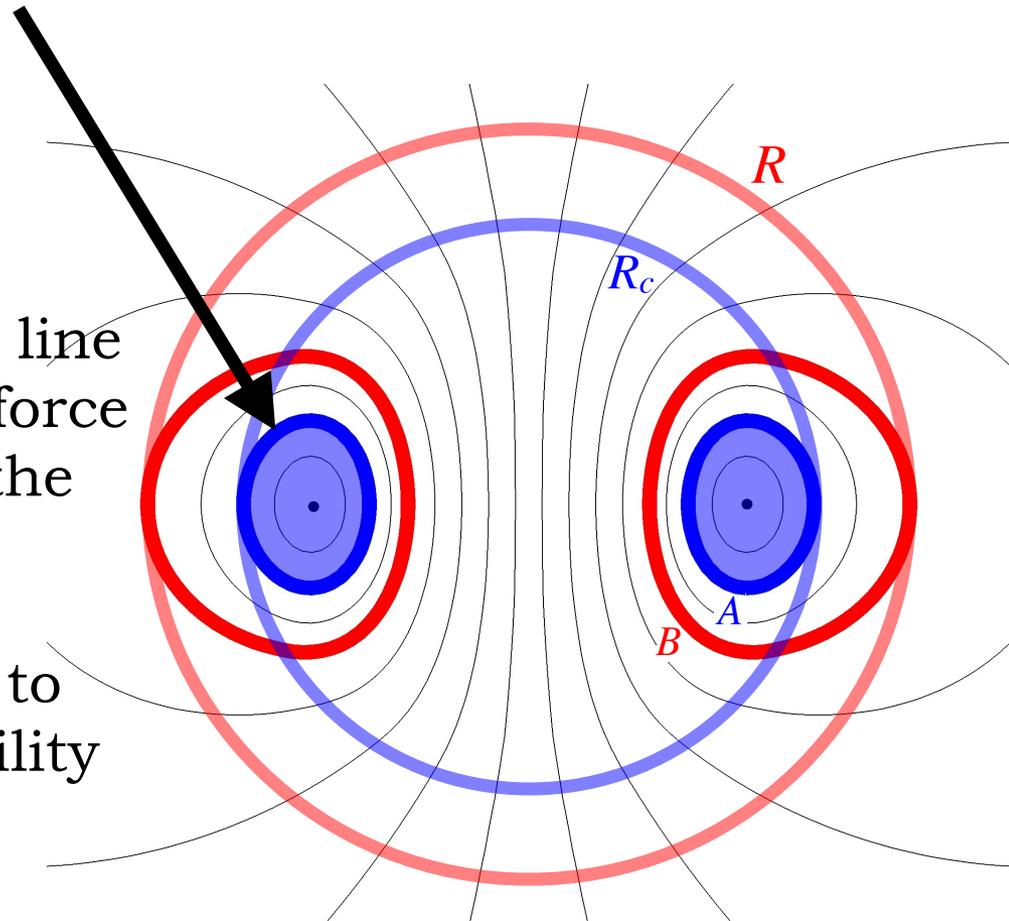


the super-rotating core region

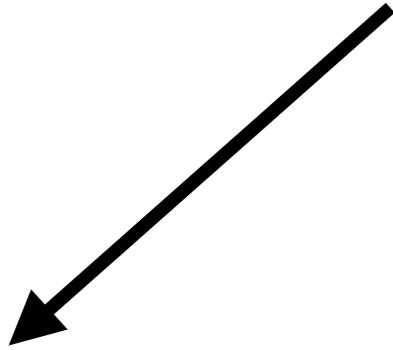
Glampedakis & PL (2015)

- Following birth, neutron stars could have a **super-rotating, torus-shaped region in the core!**

- Almost certainly unstable:
 - velocity jump along field line A induces local Lorentz force that will try to displace the super-rotating region
 - also should be unstable to Kelvin-Helmholtz instability



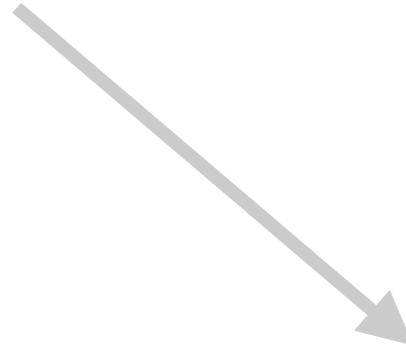
Two Possible Outcomes



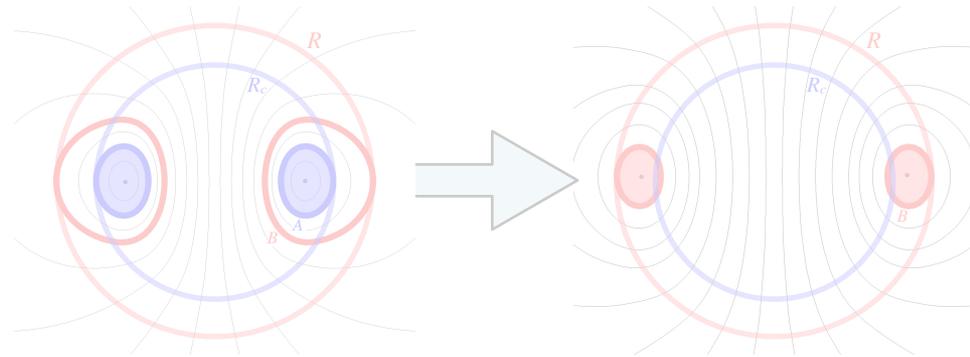
i) core remains in constant turbulent state



Peralta, Melatos, et al.



ii) magnetic field evicted to crust



Turbulent Consequences

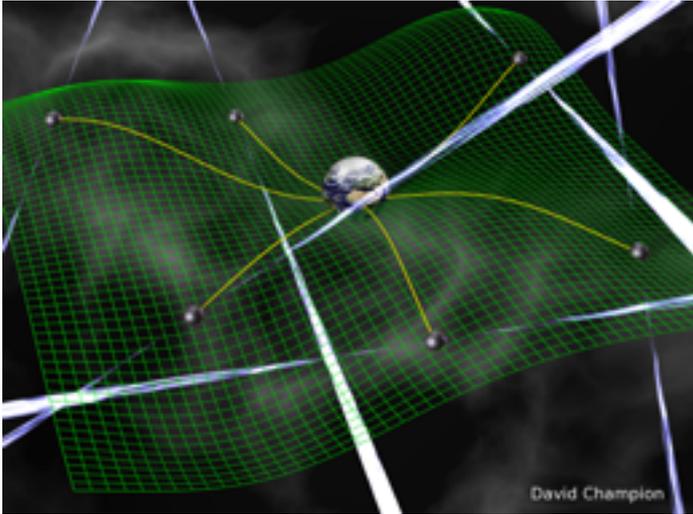
→ Pulsar timing noise

- Is pulsar timing noise from turbulence?
- Quantifying the effect on gravitational wave detection with Pulsar Timing Arrays

→ Gravitational waves - LIGO

- Single Neutron Star
- Stochastic Background

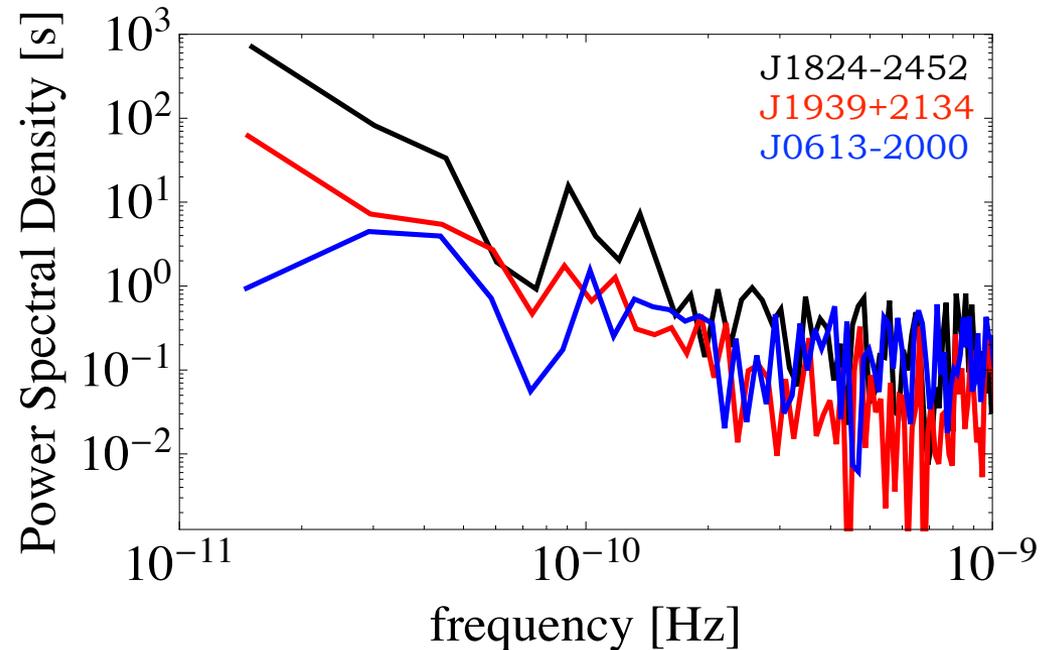
Pulsar Timing Arrays



- Time millisecond pulsars with **EXTREME** precision
- Look for correlated timing residuals as GW signature
 - **Timing Residual: difference between measured and modelled phase of pulse.**

→ Timing noise:

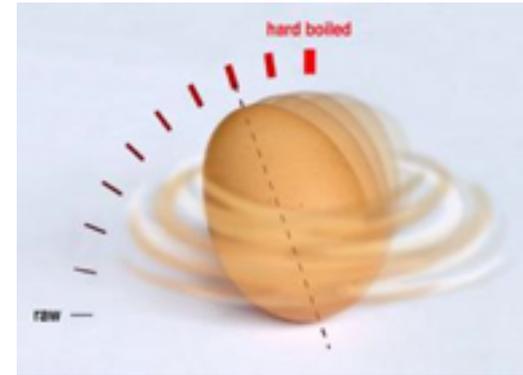
- Stochastic wandering of pulse arrival times
- stochastic torque fluctuations exerted on crust by turbulent fluid in core



Timing Noise Due to Turbulence

Greenstein
(1970; Nature)

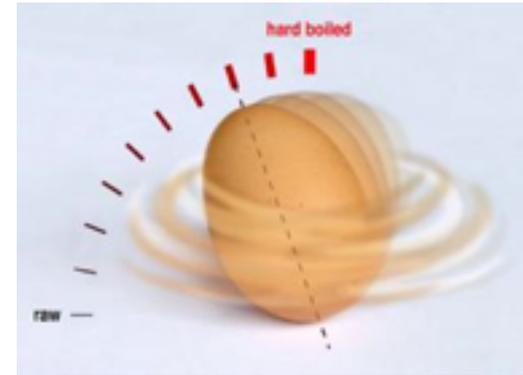
‘My final point is a speculative one. When an uncooked egg rotates it does so irregularly. The yolk inside moves about erratically, and in order to conserve angular momentum the rotation rate of the shell must also fluctuate. The rotating turbulent neutron superfluid must exhibit something like the same phenomenon.



Timing Noise Due to Turbulence

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(1970; Nature)

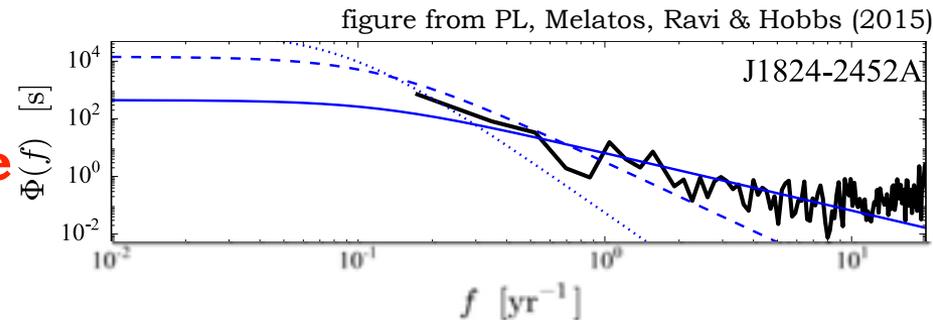
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Melatos & Link (2014)

**calculated angular momentum
fluctuations on NS crust from core**

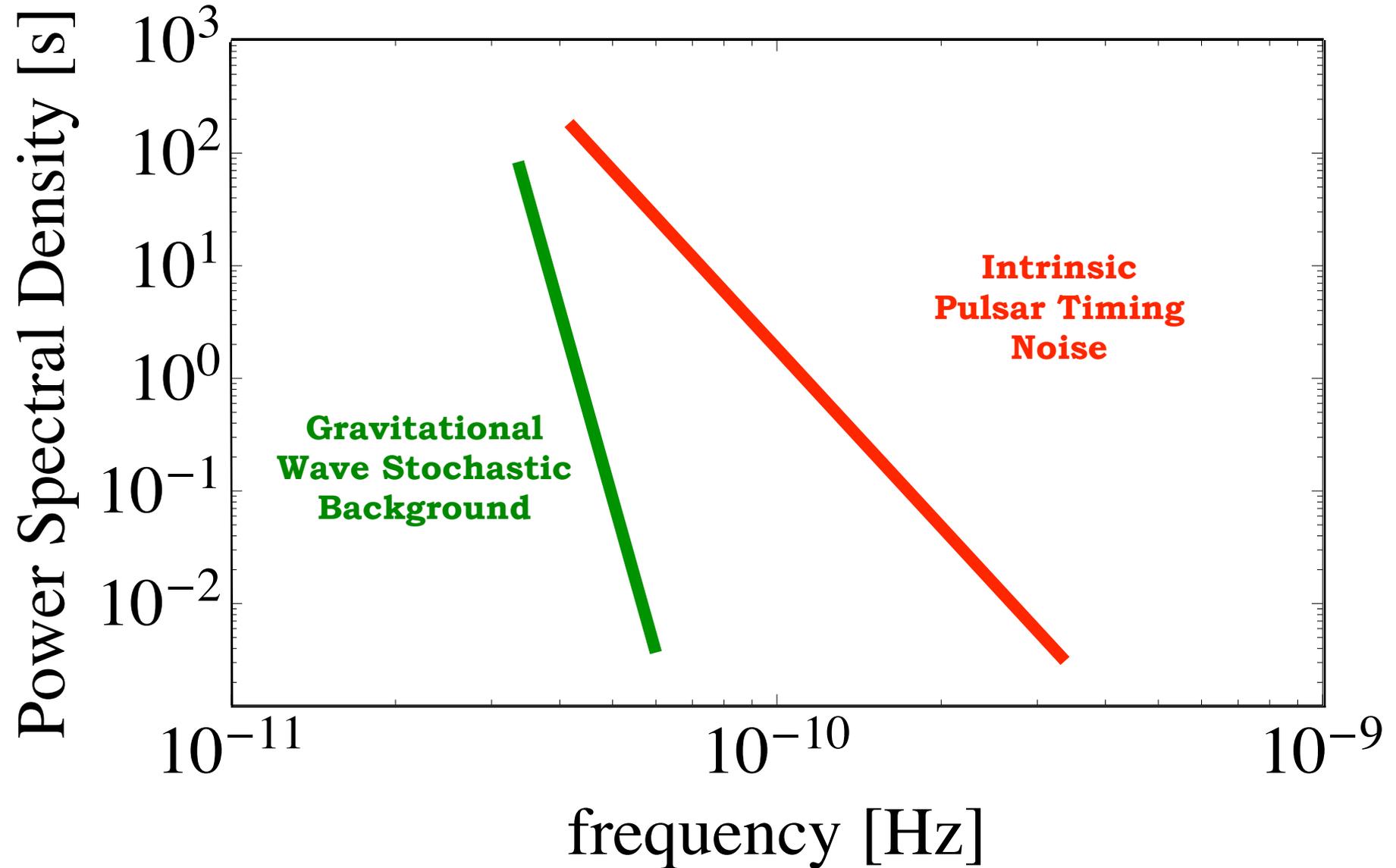
**Small number of (relatively
unconstrained) parameters ‘fit’
timing noise spectra.**



**Prediction: low-frequency
plateau in timing noise spectrum**

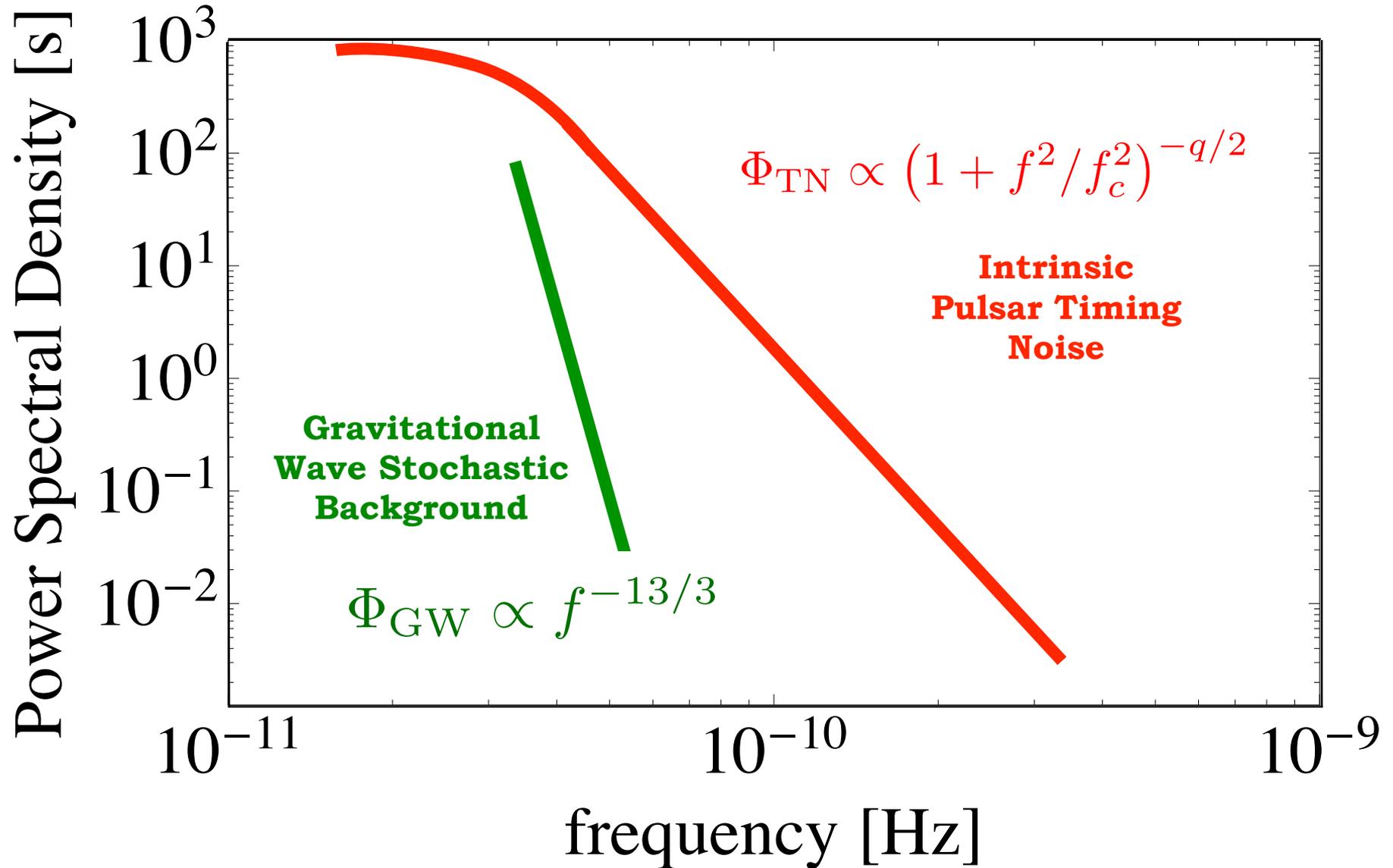
Quantifying the effect on GW detection with PTAs

PL, Melatos, Ravi & Hobbs (2015)



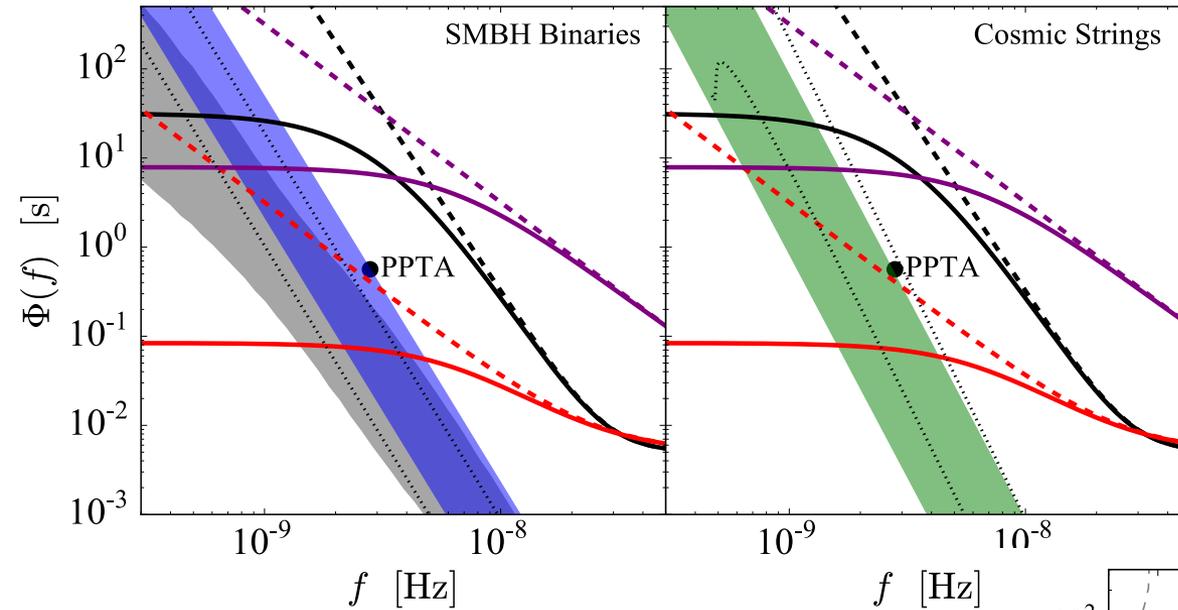
Quantifying the effect on GW detection with PTAs

PL, Melatos, Ravi & Hobbs (2015)



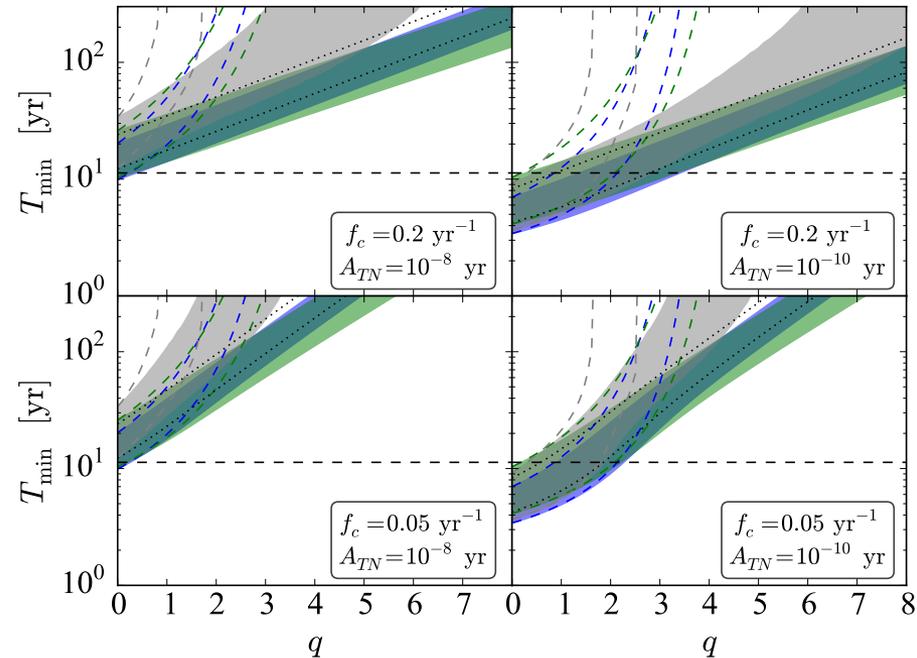
Quantifying the effect on GW detection with PTAs

PL, Melatos, Ravi & Hobbs (2015)



→ Punch line:

- A low-frequency turnover is great for PTAs
- evidence for one is hard to find

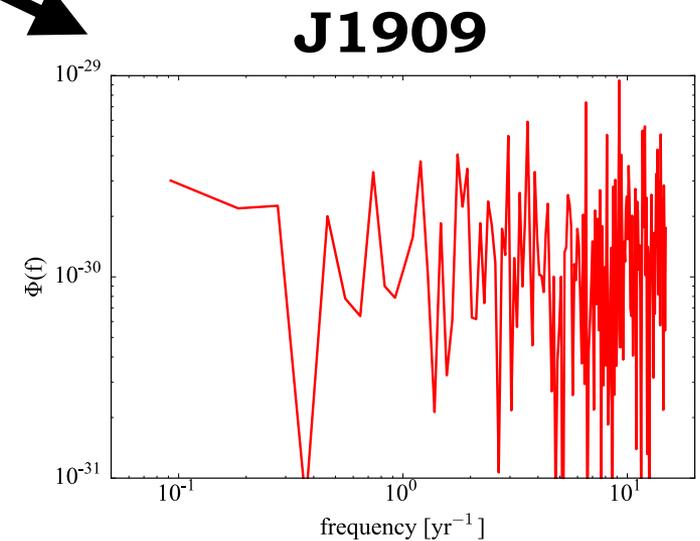
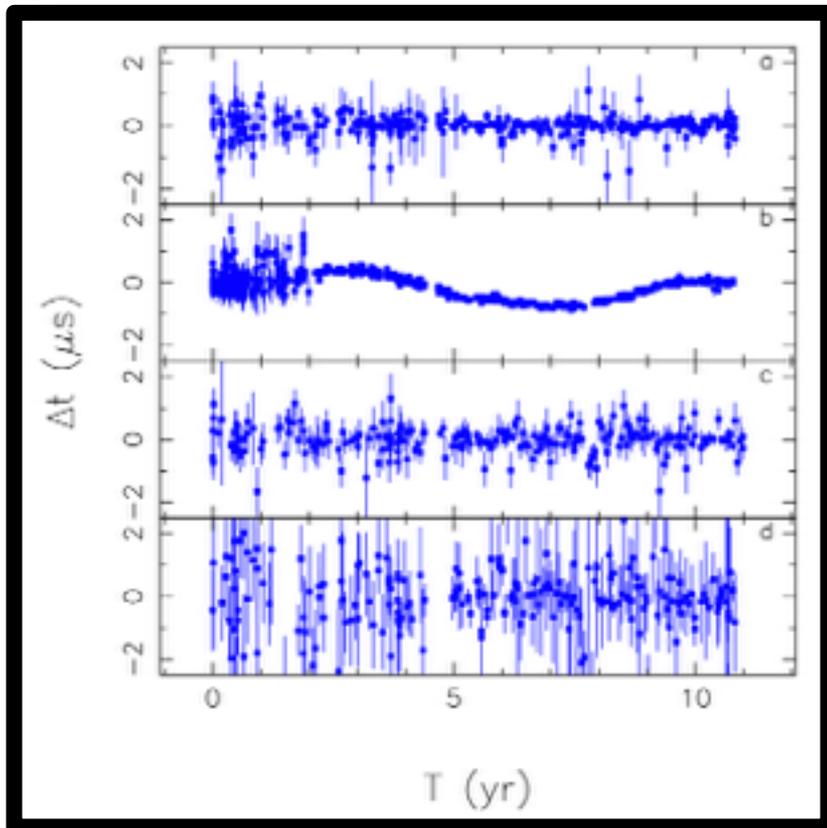


Quantifying the effect on GW detection with PTAs

This may not matter for a number of years...

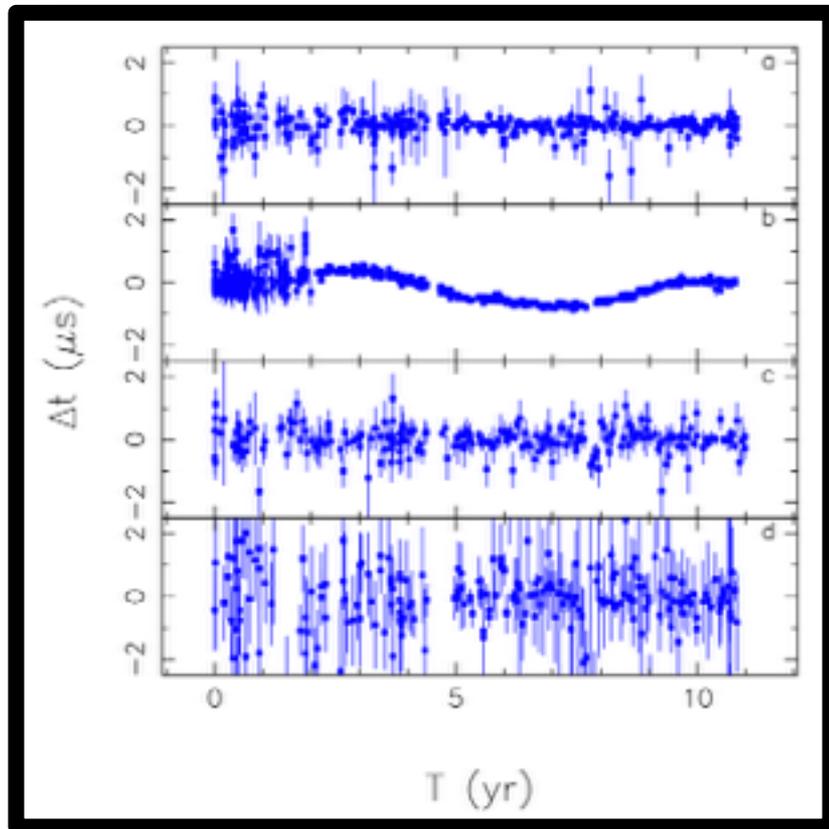
Shannon et al. (in prep)

Bayesian analysis: No evidence for red noise in the two pulsars that are biggest contributors to new GW limit

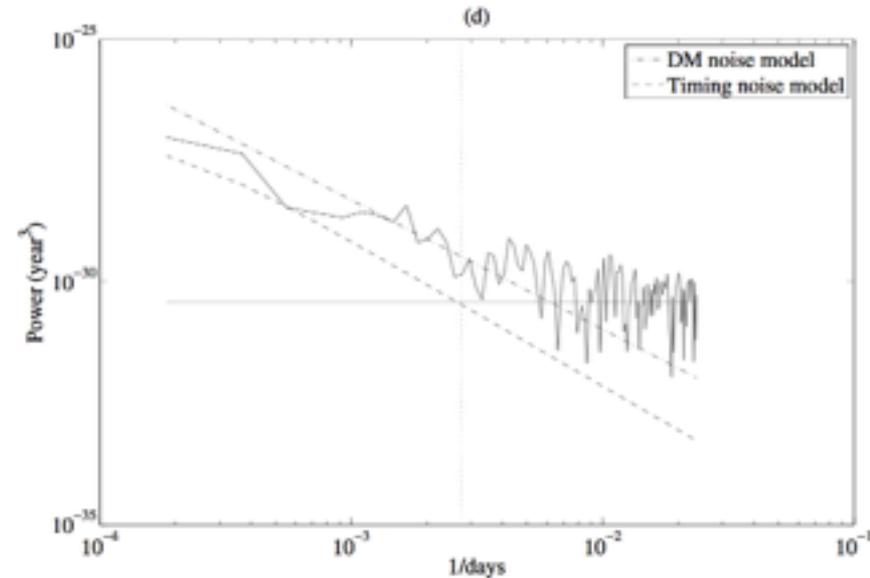


What about the level of red noise?

Red noise in PSR0437 is *NOT* a gravitational wave background!



J0437



Reardon et al. (in prep)

Search for evidence of a plateau in the spectrum to (potentially) understand neutron star core physics!

Turbulent Consequences

→ Pulsar timing noise

- Is pulsar timing noise from turbulence?
- Quantifying the effect it has on gravitational wave detection with PTAs

→ Gravitational waves - LIGO

- Single Neutron Star
- Stochastic Background

Turbulent flows emit gravitational waves

Melatos & Peralta (2010)

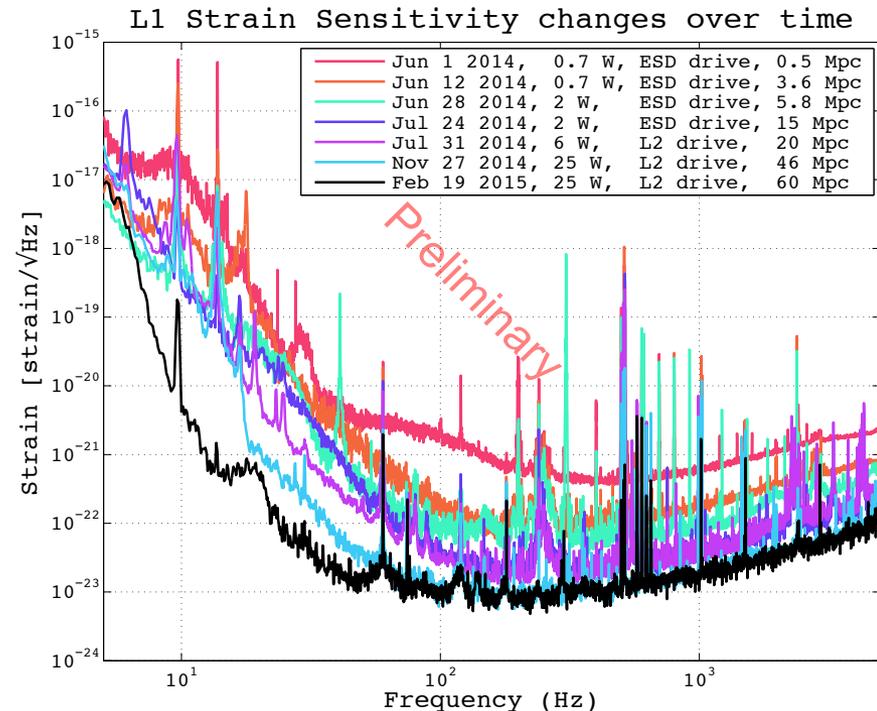
Turbulence: On average - axisymmetric

Instantaneously non-axisymmetric

$$h_{\text{rms}} = 5 \times 10^{-28} \left(\frac{M_{\star}}{1.4 M_{\odot}} \right) \left(\frac{R_{\star}}{10 \text{ km}} \right)^3 \left(\frac{d}{1 \text{ kpc}} \right)^{-1} \left(\frac{\Delta\Omega}{10 \text{ rad s}^{-1}} \right)^3$$

Shear
 ← (difference in angular velocity between crust and core)

Only of potential interest to LIGO for nearby ($d \sim 10 \text{ pc}$) fast rotators ($P \sim 1 \text{ ms} \Rightarrow \Delta\Omega \sim 30$)



One neutron star does not emit a detectable gravitational wave signal

What about ALL the neutron stars in the Universe?

PL, Bennett & Melatos (2013)

Consider 2 Populations

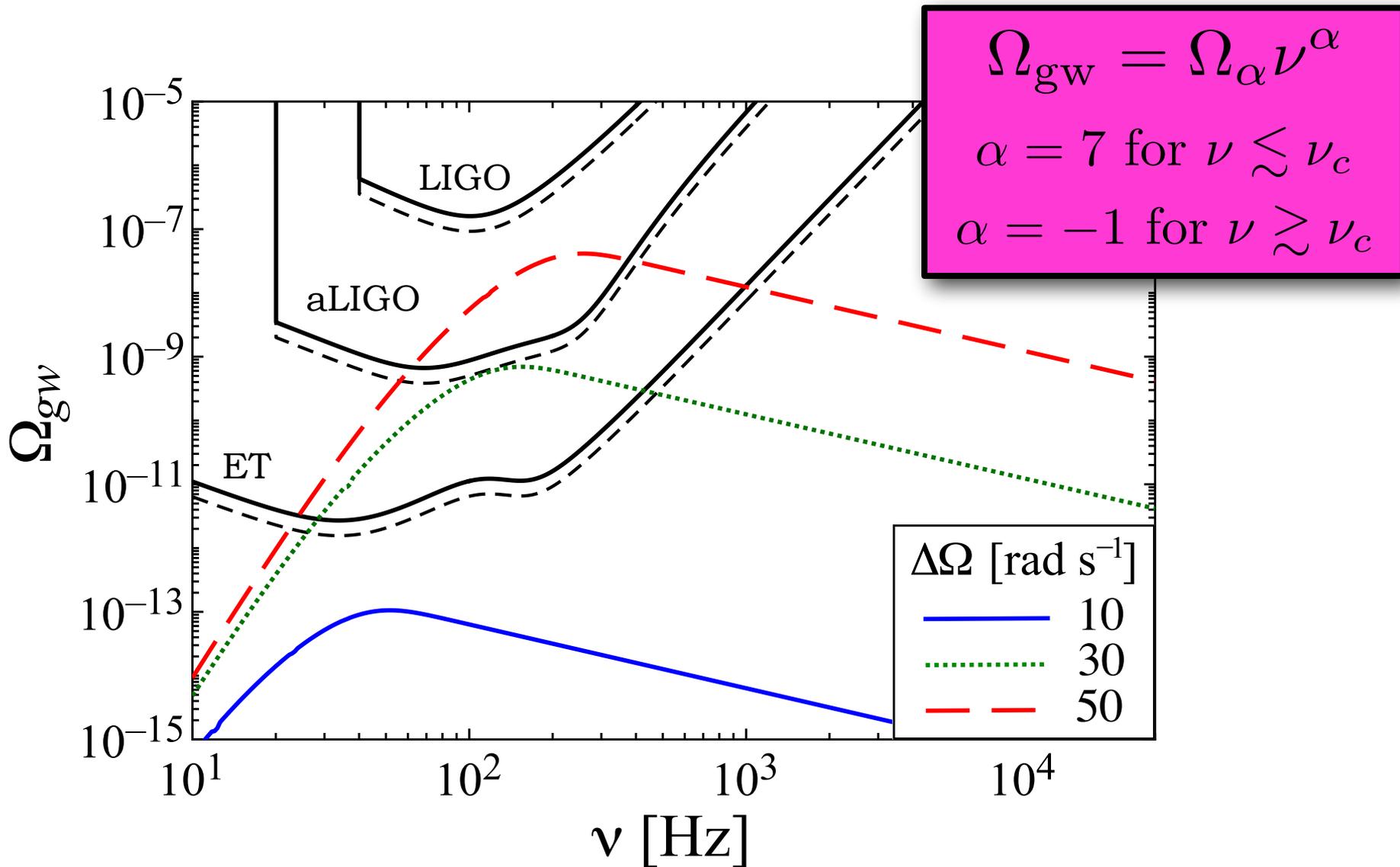
➔ **Naive:**

➔ all NSs in Universe have same $\Delta\Omega$. i.e. $\Delta\Omega$ is independent of Ω

➔ **Radio pulsars:**

➔ Broad distribution of $\Delta\Omega$, where $\Delta\Omega$ is proportional to spindown rate

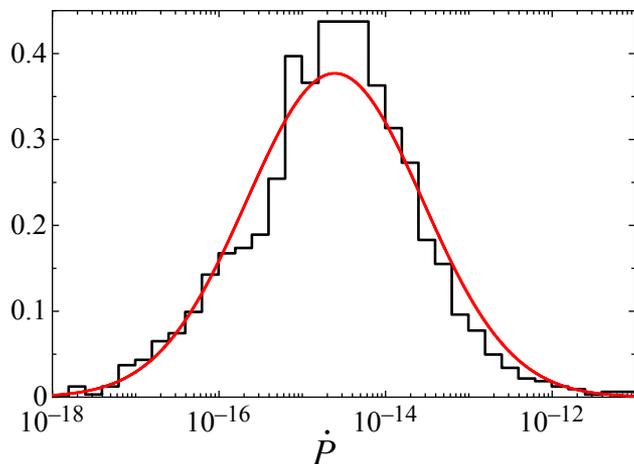
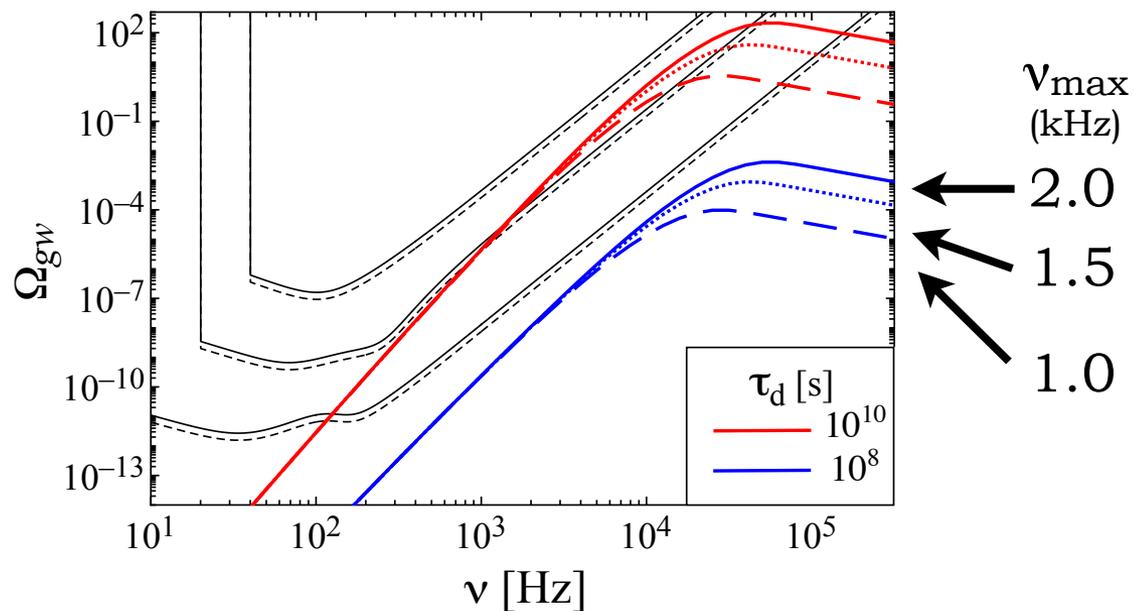
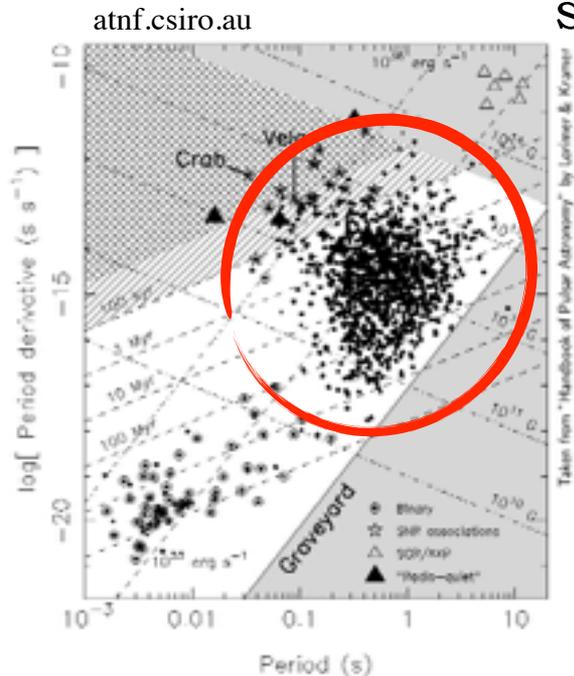
Unique $\Delta\Omega$



Pulsar Population

take galactic distribution of known pulsars and assume the same throughout the Universe

$$\Delta\Omega = \tau_d \dot{\Omega}$$



Detection unlikely

“Things sometimes happen to me that are very, very unlikely. Does it mean that I don't exist with high Bayesian probability?”
(Levin 2015, Facebook)

Non-detections give interesting constraints on shear damping times, etc.

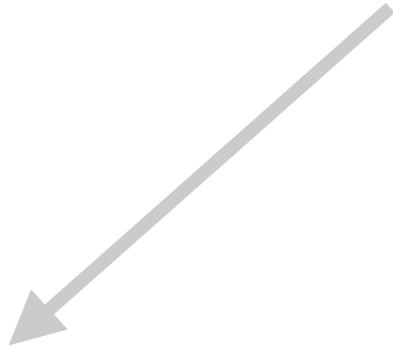
$$\Omega_{\text{gw}} = \Omega_{\alpha} \nu^{\alpha}$$

$$\alpha = 7 \text{ for } \nu \lesssim \nu_c$$

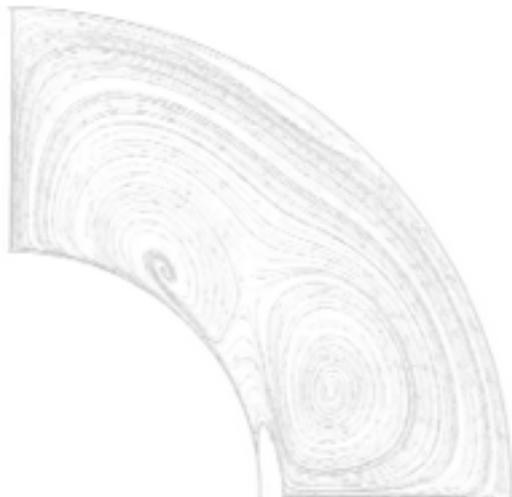
$$\alpha = -1 \text{ for } \nu \gtrsim \nu_c$$

It is worth searching for this.

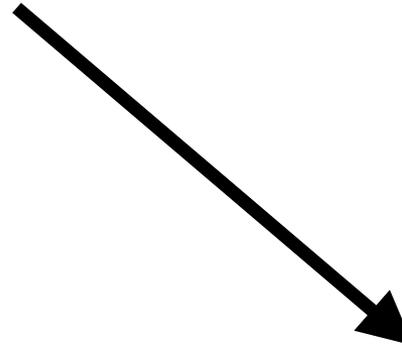
Two Possible Outcomes



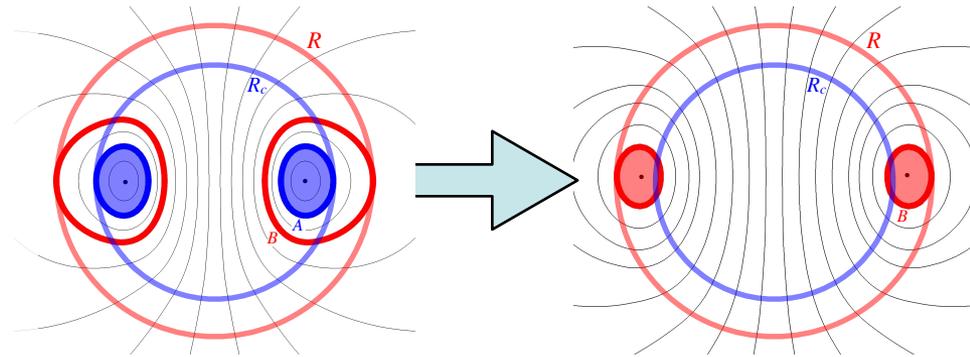
i) core remains in constant turbulent state



Peralta, Melatos, et al.



ii) magnetic field evicted to crust

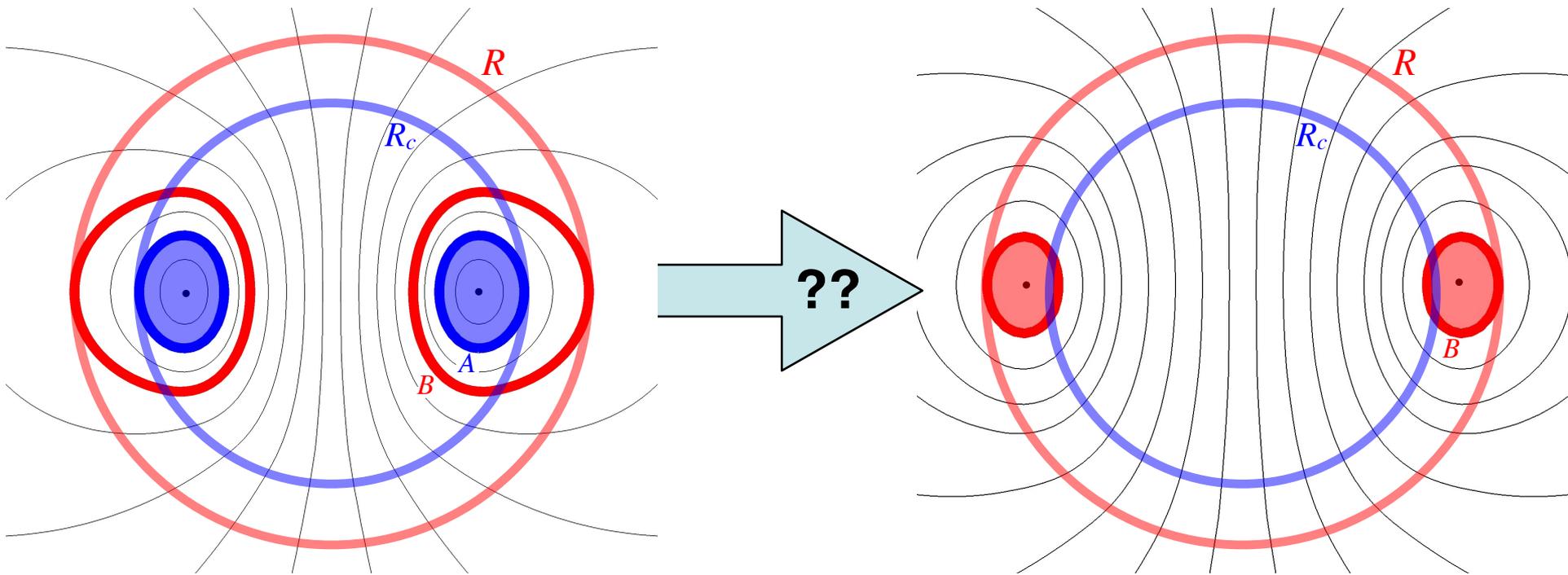


the crust as a magnetic field depository

Glampedakis & PL (2015)

- A Conjecture:

the system will evict the closed field lines + toroidal region into the crust

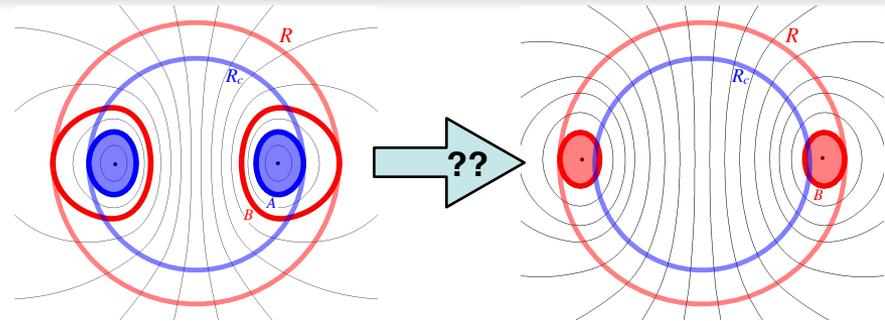


the crust as a magnetic field depository

Glampedakis & PL (2015)

- A Conjecture:

the system will evict the closed field lines + toroidal region into the crust



- *young magnetars:*

$B \gtrsim 10^{15}$ G: star spins down before crust forms (~ 1 day)

$B \lesssim 10^{15}$ G: our model applies

hydrodynamic instability timescale

$$t \sim t_{sd} \approx 4.7 \left(\frac{B_p}{10^{15} \text{ G}} \right)^{-2} \left(\frac{P}{10 \text{ ms}} \right)^2 \text{ d}$$

$t \lesssim t_{sd}$: gravitational wave emission

$t \gg t_{sd}$: eviction of the magnetic field to the crust

$t \lesssim t_{\text{sd}} : \text{gravitational wave emission}$

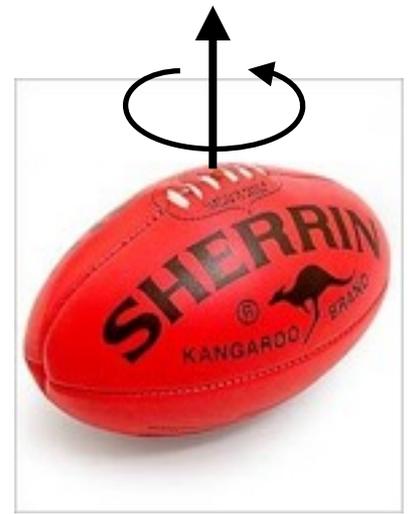
- Strong toroidal field wound up in core

$$h_0 \propto \frac{I\epsilon v^2}{D}$$

- ϵ due to magnetic deformations

$$\epsilon \sim 10^{-6} \left(\frac{B_t}{10^{15} \text{ G}} \right) \text{ e.g., Cutler (2002)}$$

Haskell et al. (2008, **erratum 2009**),
Mastrano et al. (2011)



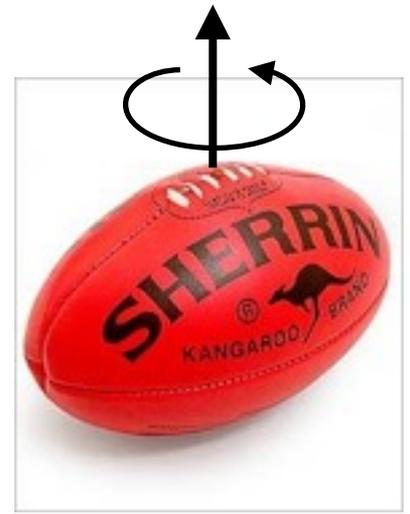
$t \lesssim t_{\text{sd}}$: gravitational wave emission

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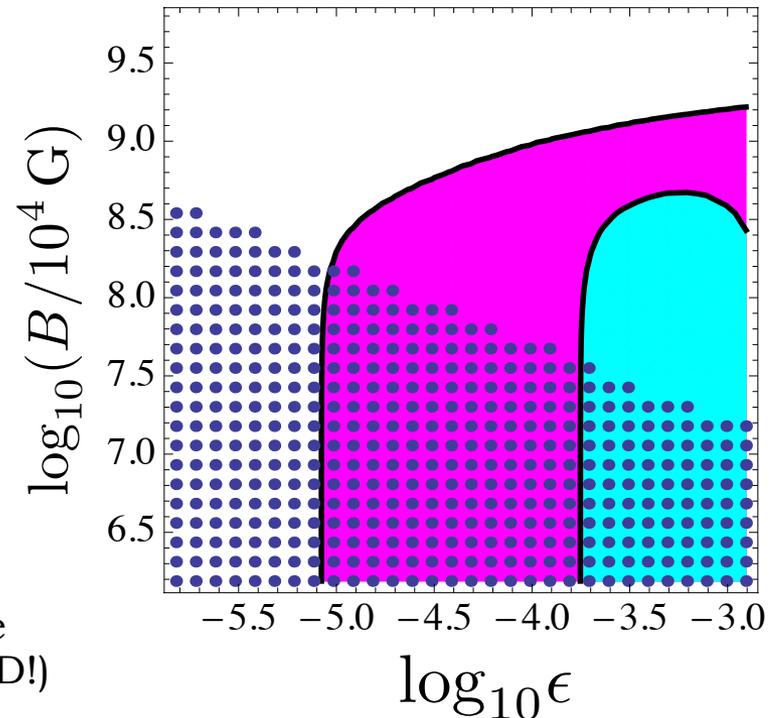
$$\epsilon \sim 10^{-6} \left(\frac{B_t}{10^{15} \text{ G}} \right) \quad \begin{array}{l} \text{e.g., Cutler (2002)} \\ \text{Haskell et al. (2008, **erratum 2009**),} \\ \text{Mastrano et al. (2011)} \end{array}$$



**unfortunately, need long
integration times:**

SN1987A: ~ 1 yr integration

Chung, Melatos, et al. (2011)



(important: other emission mechanisms possible
that make this search worthwhile — Lilli Sun's PhD!)

$t \lesssim t_{sd}$: gravitational wave

- Strong toroidal field wound

$$h_0 \propto \frac{I\epsilon v^2}{D}$$

- ϵ due to magnetic deformation

$$\epsilon \sim 10^{-6} \left(\frac{B_t}{10^{15} \text{ G}} \right) \text{ Haskell}$$

unfortunately, need long
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(important: other emission mechanisms possible
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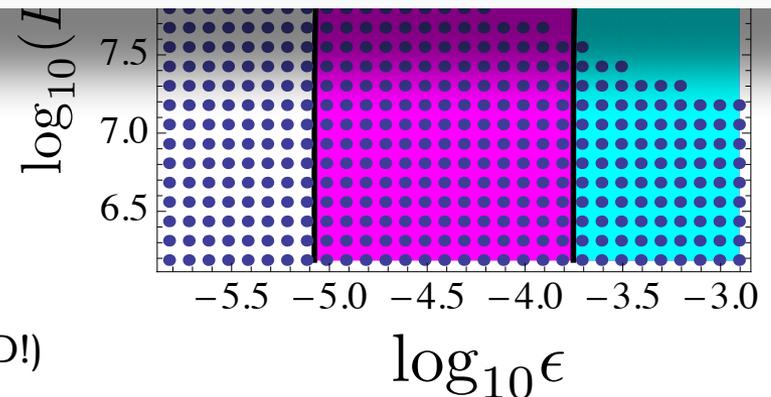
Unless....

$$\epsilon^{2SC} \sim 8.0 \times 10^{-5} \left(\frac{\langle B_t \rangle}{10^{15} \text{ G}} \right)$$

$$\epsilon^{CFL} \sim 2.5 \times 10^{-4} \left(\frac{\langle B_t \rangle}{10^{15} \text{ G}} \right)$$

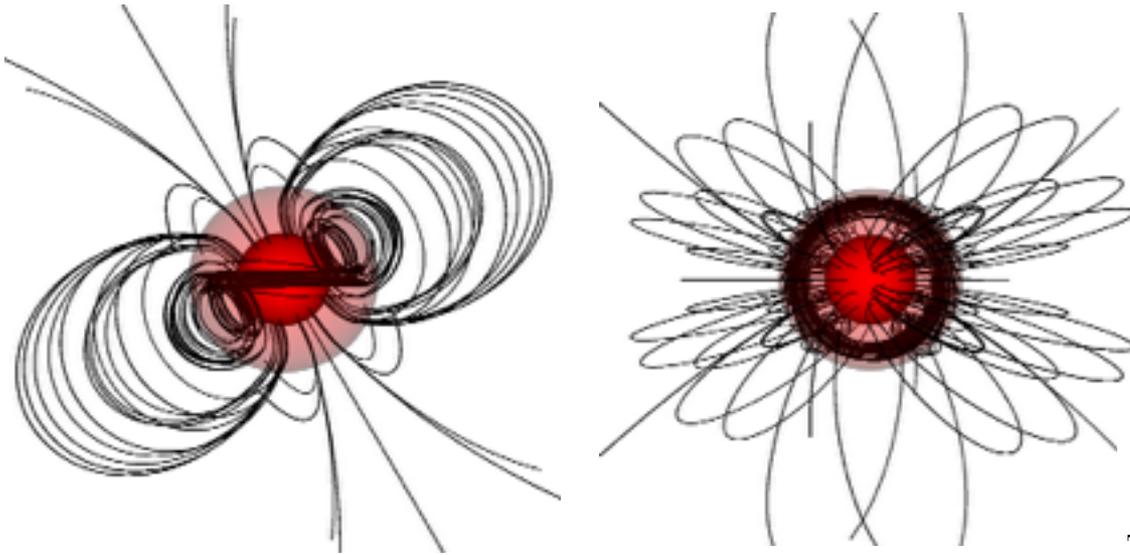
This is potentially a nuclear
physics experiment!

Owen (2004), Glampedakis et al. (2012)



$t \lesssim t_{\text{sd}}$: gravitational wave emission

- a positive detection also allows us to probe the stellar geometry (e.g., Mastrano, PL & Melatos 2013 for multipolar fields)



e.g., *twisted-torus*

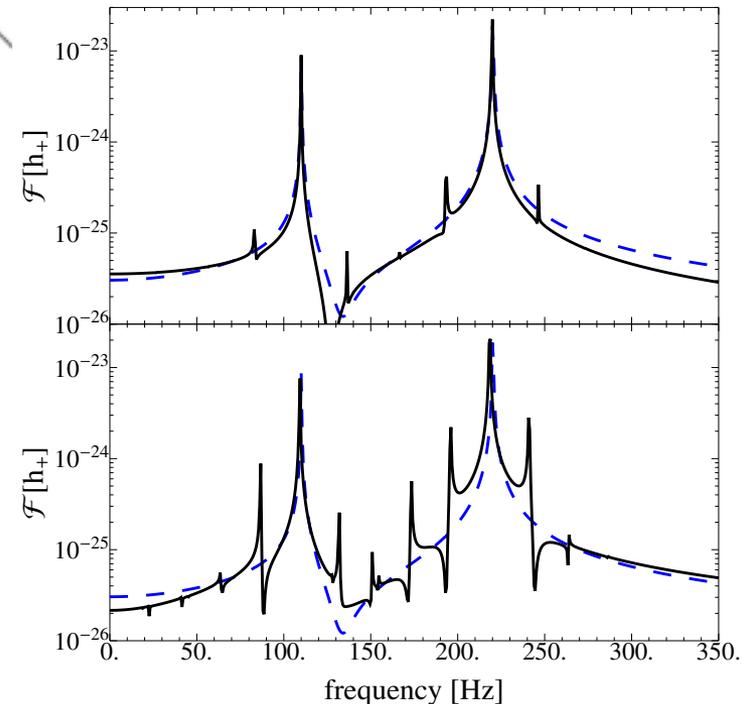
PL & Melatos (2013)

- triaxial deformation
- ‘naturally motivated’
- Enriches GW signal

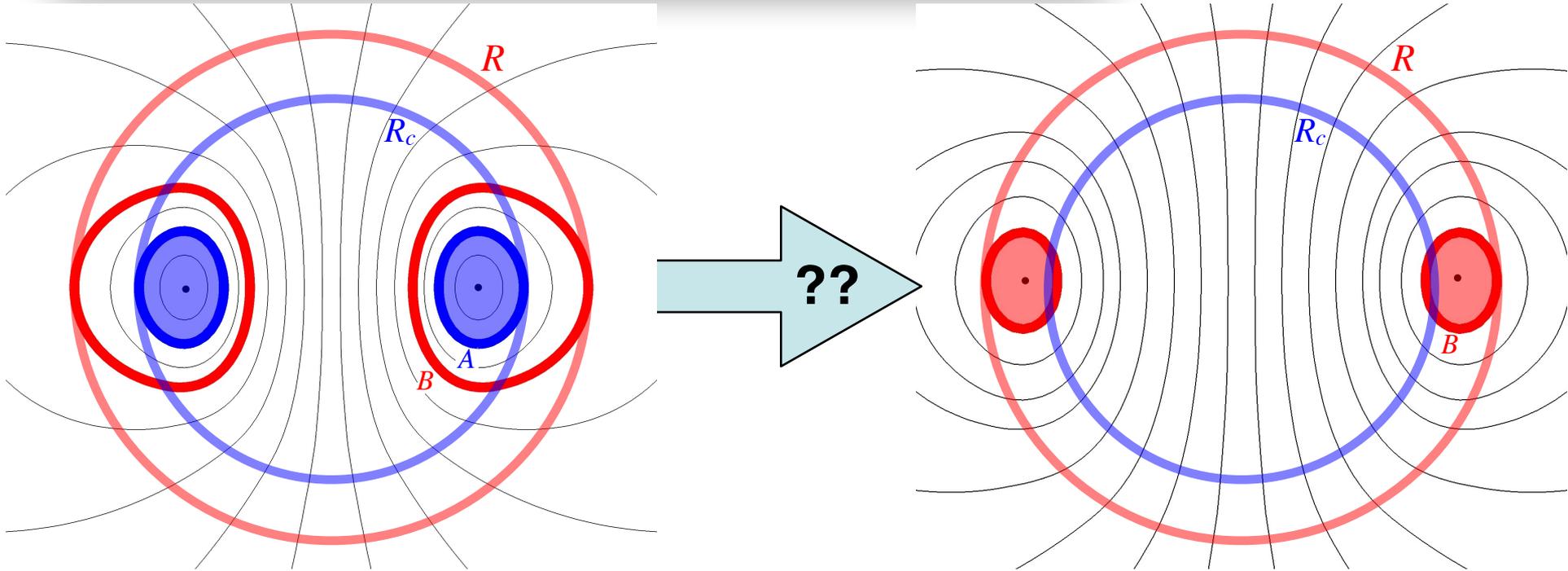
e.g., NS born with:

- Virgo cluster (~ 20 Mpc)
- $B_p = 10^{14}$ G
- $\langle B_t \rangle = 10^{16}$ G

Triaxiality must last \sim one month for SNR ~ 3 in aLIGO



$t \gg t_{sd}$: eviction of the magnetic field



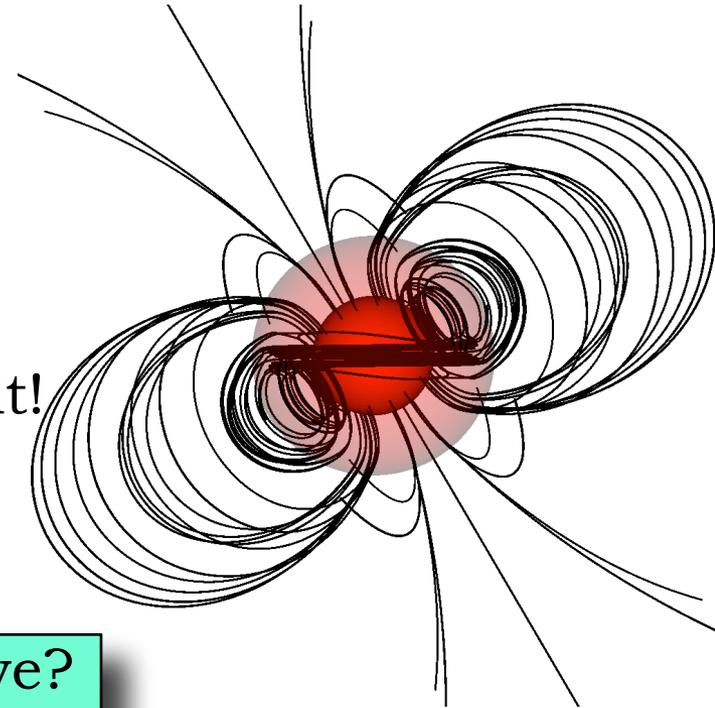
✓existence of strong toroidal field in crust is key for magnetar heating, fast magnetic evolution and flares!

the future?

magnetic field does not couple the core and crust of a neutron star.

Conjecture: *stability is reached when closed field lines + toroidal field are evicted into crust.*

- what's next?
 - more general B-field geometry
 - easy to generalise to higher-order multipoles
 - non-axisymmetric more difficult!
 - superconducting MHD



• how does the system *actually* evolve?

summary

**Crust & Core:
do they corotate? (no)**

**theoretical
implications**

A turbulent core?

**Magnetic fields in
the crust?**

**observational
implications**

**pulsar
timing
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**gravitational
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**magnetar
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