

# DUST DYNAMICS: UNLOCKING THE MYSTERIES OF PROTOPLANETARY DISCS

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*Image credit: DSHARP*

*Cosmic dust (r)evolution, EWASS 2019, 24-25th June, Lyon, France*

# THE PROBLEM



*Carina Nebula with HST (NASA/ESA/Hubble Heritage)*

*ISM: dust/gas = 1/100*



*Pinnacles desert, Western Australia (Price family)*

*Rocky planets: dust/gas  $\approx \infty$*

**How?**

# THE PHYSICS

# DRAG

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# DUST AND GAS AS MULTIPHASE MIXTURE

e.g. Harlow & Amsden (1975), Monaghan & Kocharyan (1995), Laibe & Price (2012a,b)

$$\frac{\partial \rho_g}{\partial t} + \nabla \cdot (\rho_g \mathbf{v}_g) = 0,$$

(assuming a single grain species)

$$\frac{\partial \rho_d}{\partial t} + \nabla \cdot (\rho_d \mathbf{v}_d) = 0,$$

$$\frac{\partial \mathbf{v}_g}{\partial t} + (\mathbf{v}_g \cdot \nabla) \mathbf{v}_g = -\frac{\nabla P_g}{\rho_g} + \frac{K}{\rho_g} (\mathbf{v}_d - \mathbf{v}_g) + \mathbf{f},$$

$$\frac{\partial \mathbf{v}_d}{\partial t} + (\mathbf{v}_d \cdot \nabla) \mathbf{v}_d = -\frac{K}{\rho_d} (\mathbf{v}_d - \mathbf{v}_g) + \mathbf{f},$$

No pressure term for dust

Drag terms: exchange of momentum due to gas-dust collisions

# THE “STOPPING TIME”

$$\frac{\partial \Delta \mathbf{v}}{\partial t} = - \frac{\Delta \mathbf{v}}{t_{\text{stop}}}$$

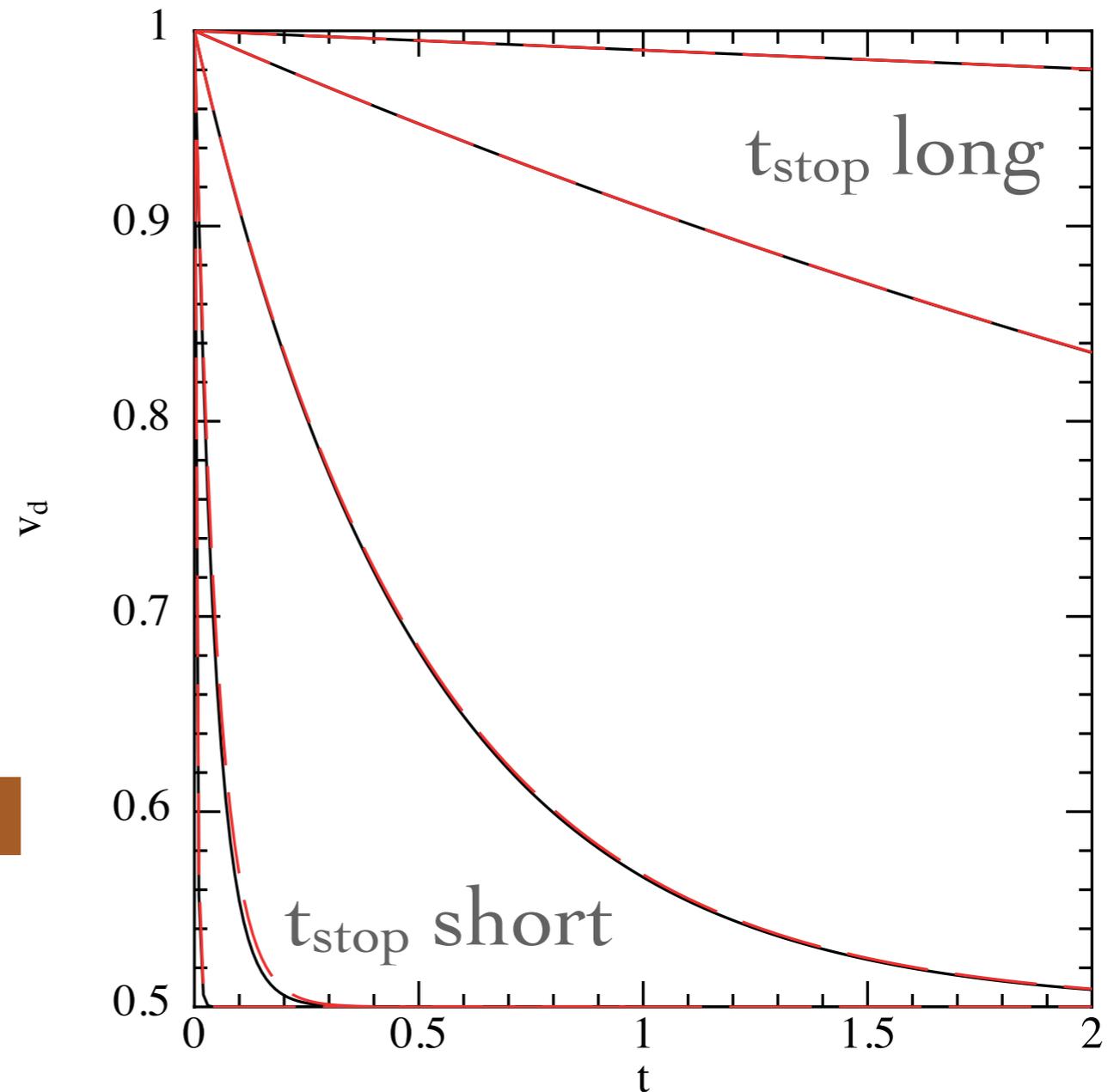
Differential velocity between gas and dust

$$t_{\text{stop}} \equiv \frac{\rho_d \rho_g}{K(\rho_d + \rho_g)}$$

Characteristic timescale for exponential decay

$$t_{\text{stop}} = \frac{\rho_{\text{gr}} s}{\rho c_s}$$

Proportional to grain size /  
Inversely proportional to gas density



“Dustybox” problem from Laibe & Price (2011)

**$T_{\text{STOP}}$  CAN GO FROM ZERO  
TO INFINITY**



# ONE FLUID DUST/GAS

*Laibe & Price (2014a,b,c), Price & Laibe (2015),  
Hutchison et al. (2018), Ballabio et al. (2018)*

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- Rewrite equations with dust fraction, total density, drift velocity
- Assume short stopping time / low  $St$  / large drag, get:

$$\frac{d\rho}{dt} = -\rho(\nabla \cdot \mathbf{v})$$

$$\frac{d\mathbf{v}}{dt} = -\frac{\nabla P}{\rho} + \mathbf{f}$$

$$\frac{d\epsilon}{dt} = -\frac{1}{\rho} \nabla \cdot (\epsilon t_s \nabla P)$$

$$\epsilon \equiv \frac{\rho_d}{\rho}$$

- Can use explicit timesteps even when stopping time is short
- Easily extended to multi-grain populations (Laibe & Price 2014c, Hutchison et al. 2018), implemented in PHANTOM SPH code (Price et al. 2018; <http://bitbucket.org/danielprice/phantom>)

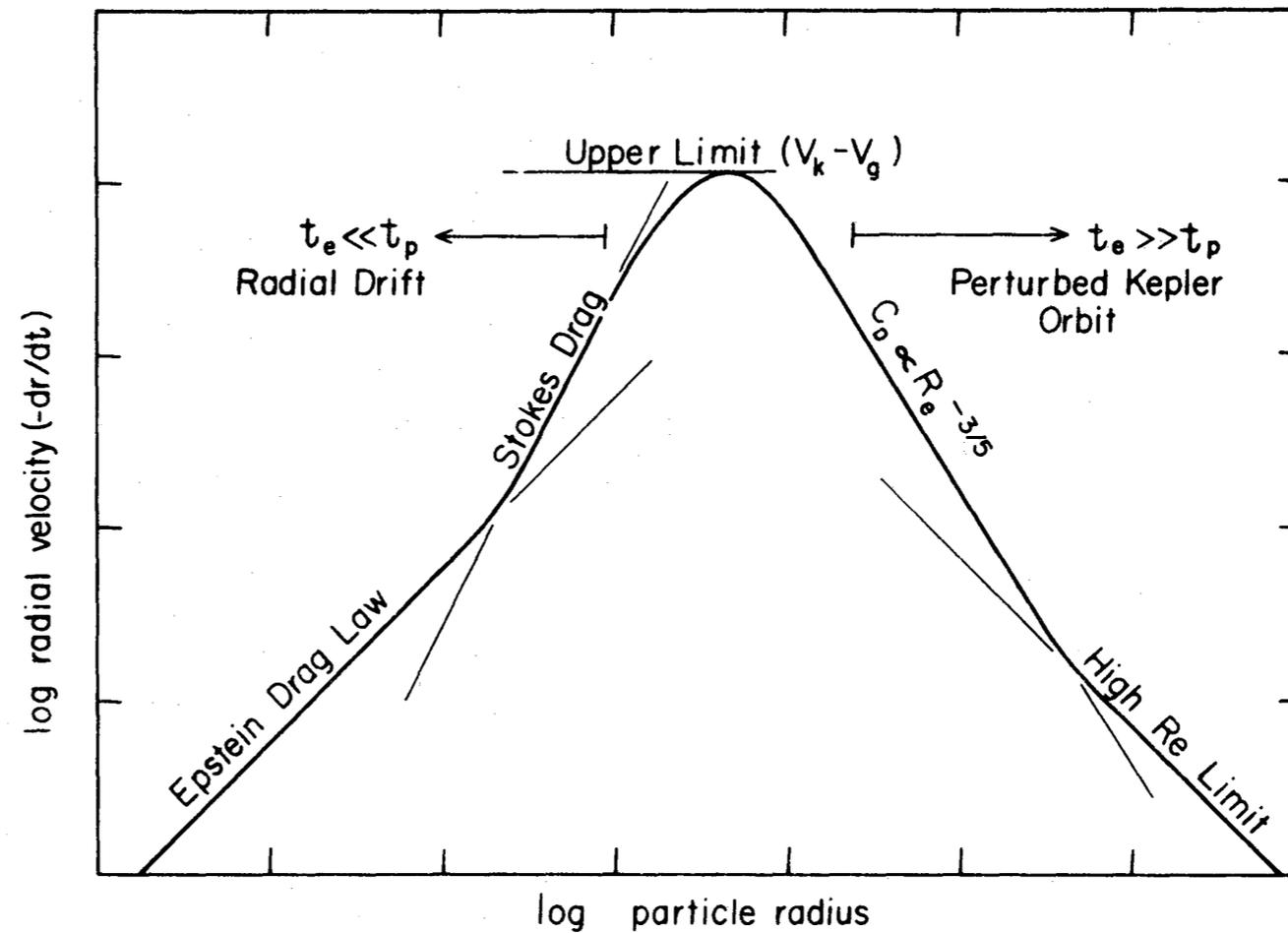


# STOKES NUMBER

Weidenschilling (1977)

$$t_{\text{stop}} = \frac{\rho_{\text{gr}} S}{\rho c_s}$$

$$S_t = t_{\text{stop}} \Omega$$



**Figure 1.** Radial velocity versus particle size (schematic). The shape of the curve is determined by the drag laws, but the peak value depends only on the nebular structure.

# DUST BEHAVIOUR IN DISCS DEPENDS ON GAS COLUMN DENSITY

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The diagram shows the equation for dust settling time  $S_t$  with three labels in brown boxes pointing to variables in the equation:

- Gas column density** points to  $\Sigma$
- Grain composition** points to  $\rho_{\text{grain}}$
- Grain size** points to  $s$

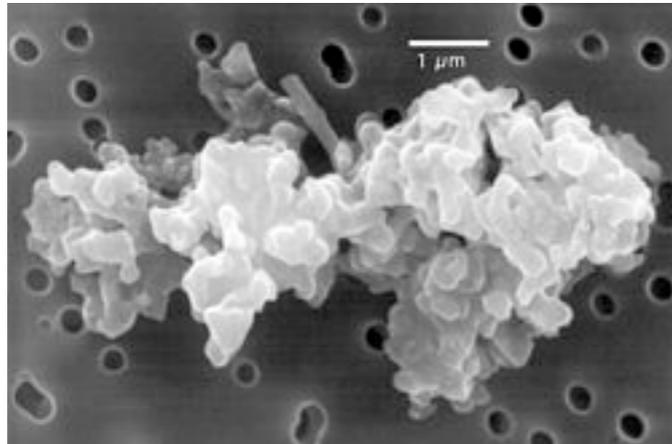
$$S_t = 1 \left( \frac{\Sigma}{0.2 \text{g/cm}^2} \right)^{-1} \left( \frac{\rho_{\text{grain}}}{3 \text{g/cm}^3} \right) \left( \frac{s}{1 \text{mm}} \right) \left( \frac{f}{1} \right)^{-1}$$

*Dipierro et al. (2015)*

*No dependence on stellar mass or mass of dust disc!*

# PHYSICS I WILL NOT DISCUSS: GRAIN GROWTH

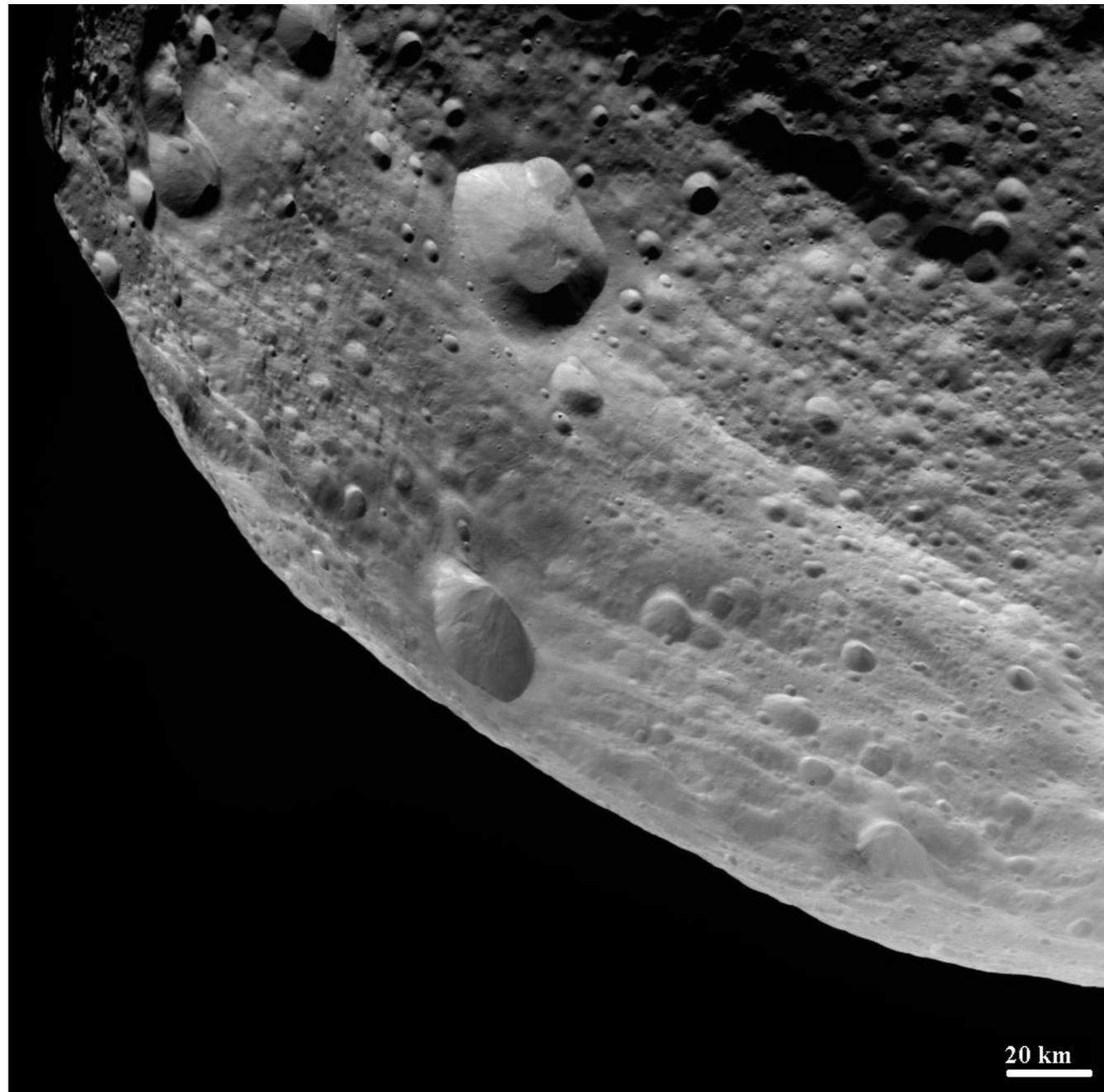
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en.wikipedia.org



Image: Gemini  
Observatory/AURA  
Artwork by Lynette Cook



# FROM 0.01 TO INFINITY

**After explaining to a student through various lessons and examples that:**

$$\lim_{x \rightarrow 8} \frac{1}{x-8} = \infty$$

**I tried to check if he really understood that, so I gave him a different example.**

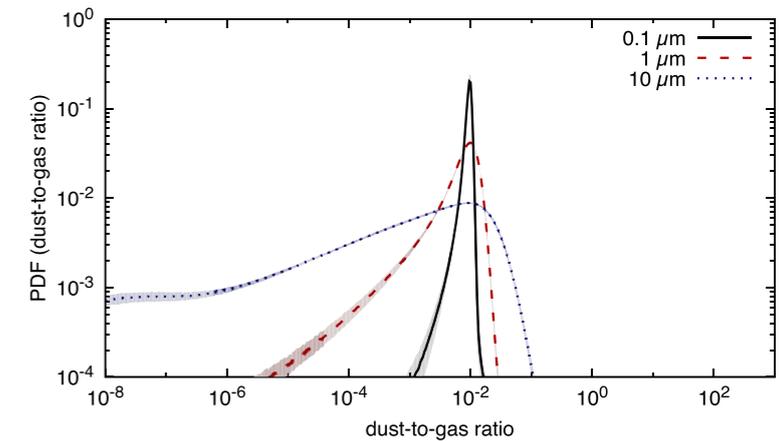
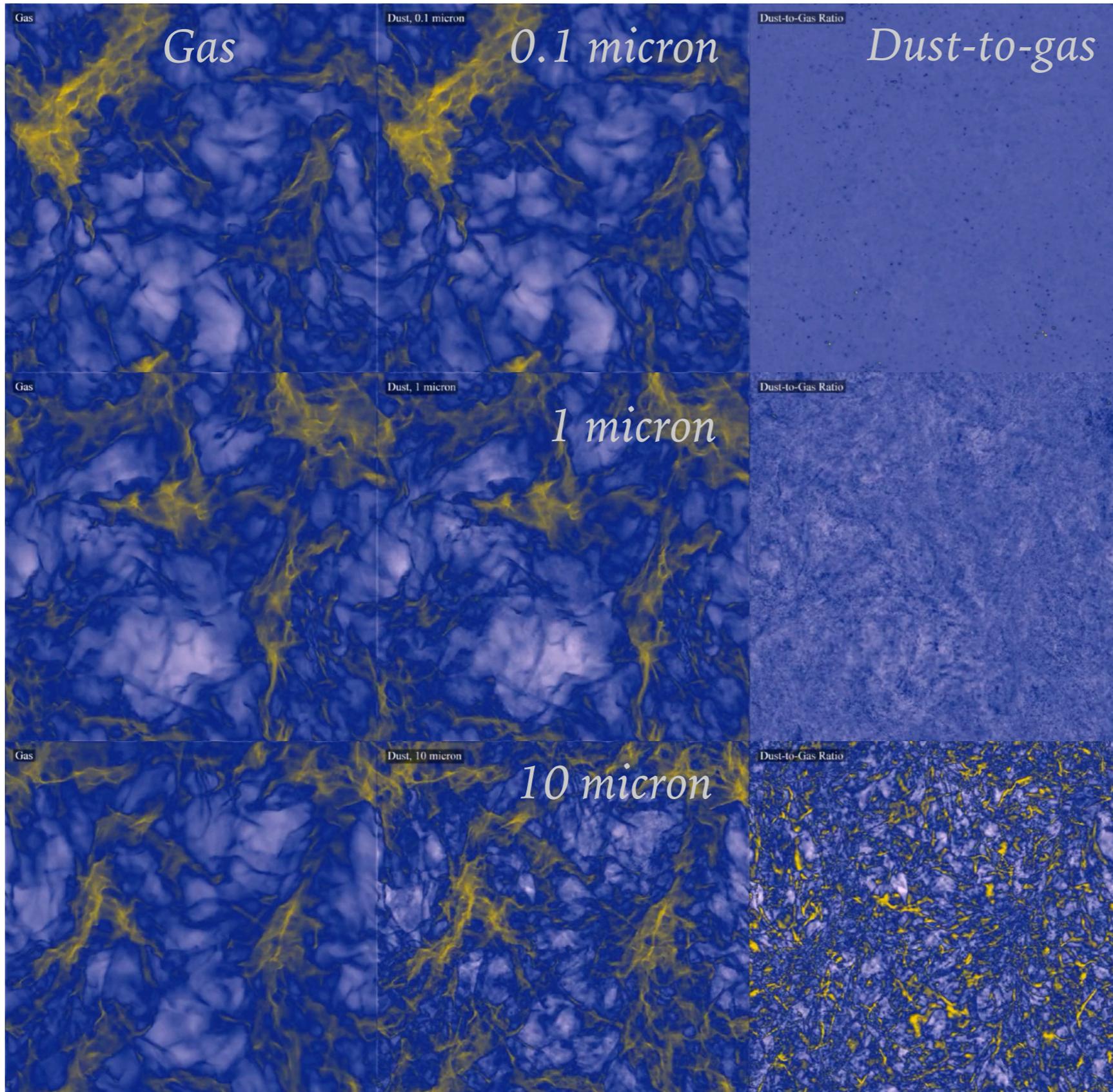
**This was the result:**

$$\lim_{x \rightarrow 5} \frac{1}{x-5} = \infty$$

*Credit: bad internet jokes*

# IS THE DUST TO GAS RATIO CONSTANT IN MOLECULAR CLOUDS?

*Tricco, Price & Laibe (2017)*



Dynamical size-sorting of grains

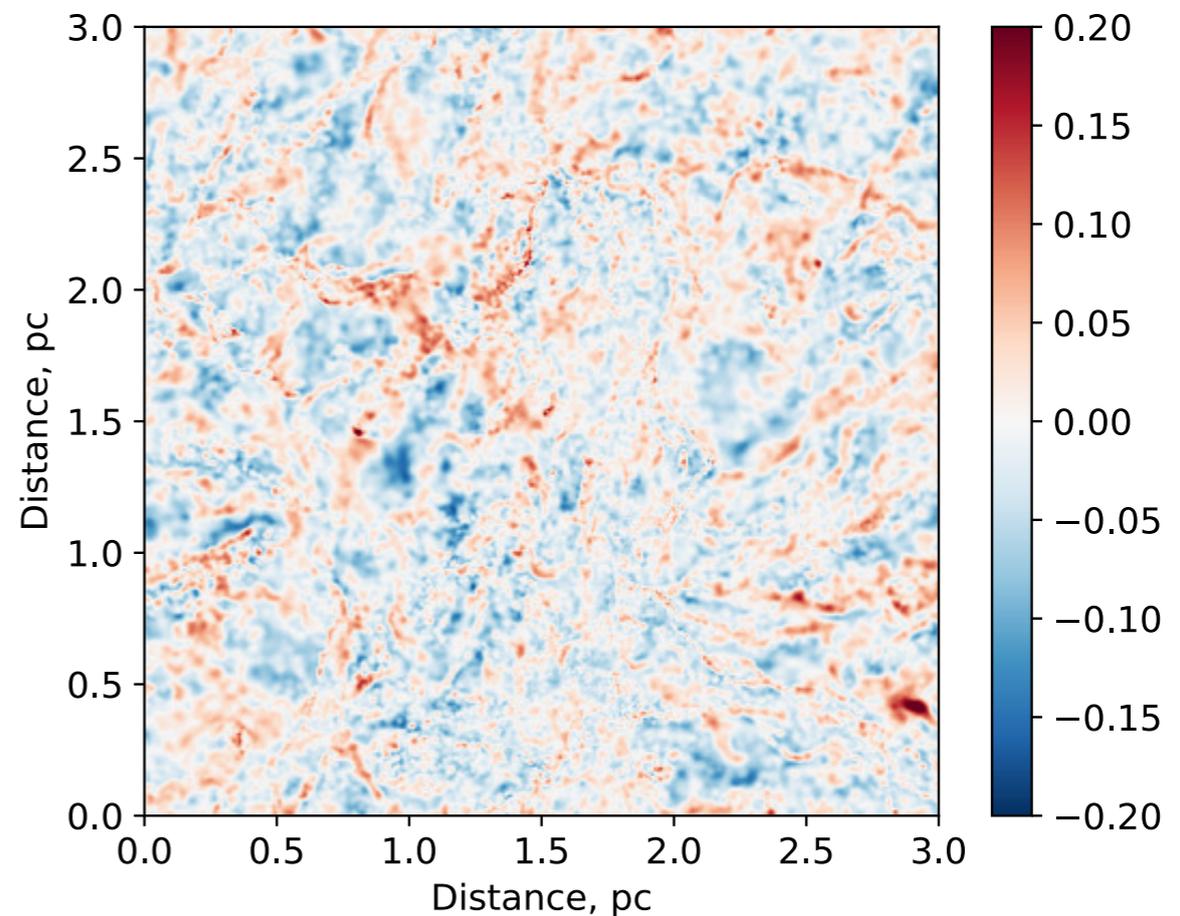
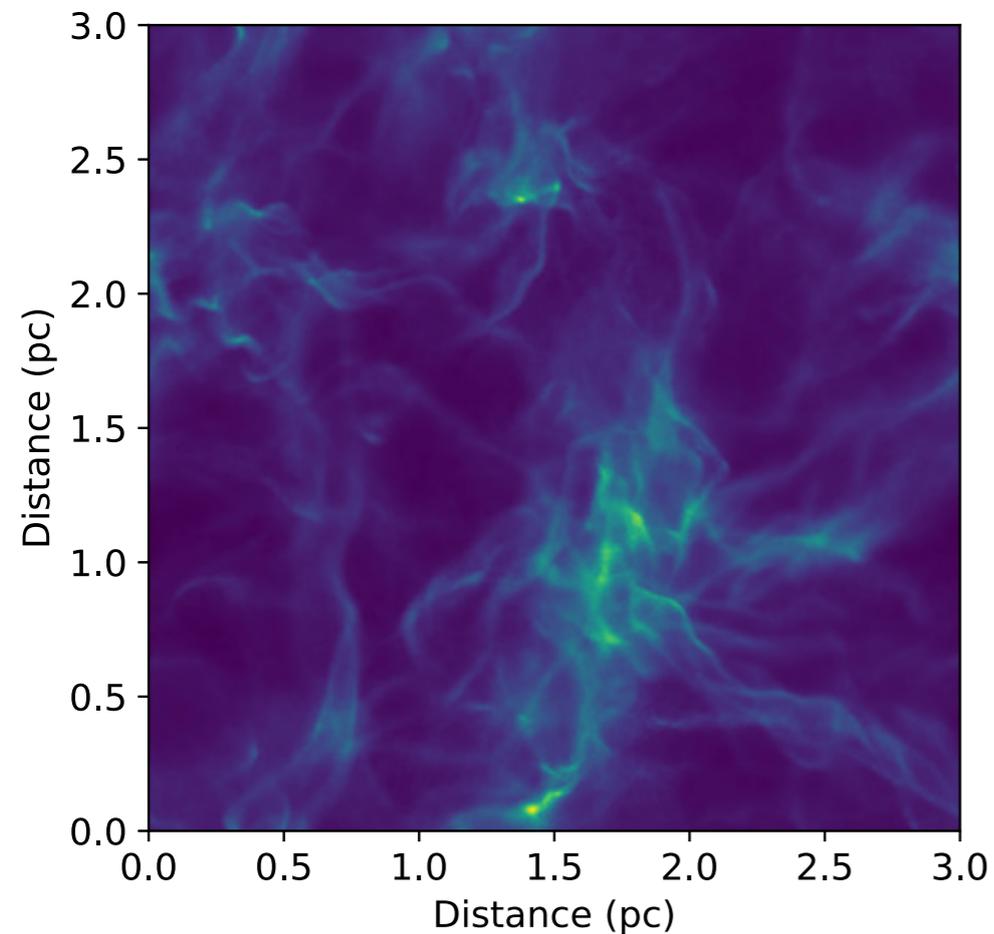
Decoupling of grains begins in the ISM!

*(but no stars made of metal...)*

# DYNAMICAL SORTING OF GRAINS

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*Credit: Tom Maunder*



Change in power-law slope  
caused by dynamical sorting  
(from MRN)

*Price, Laibe, Maunder, in prep.*

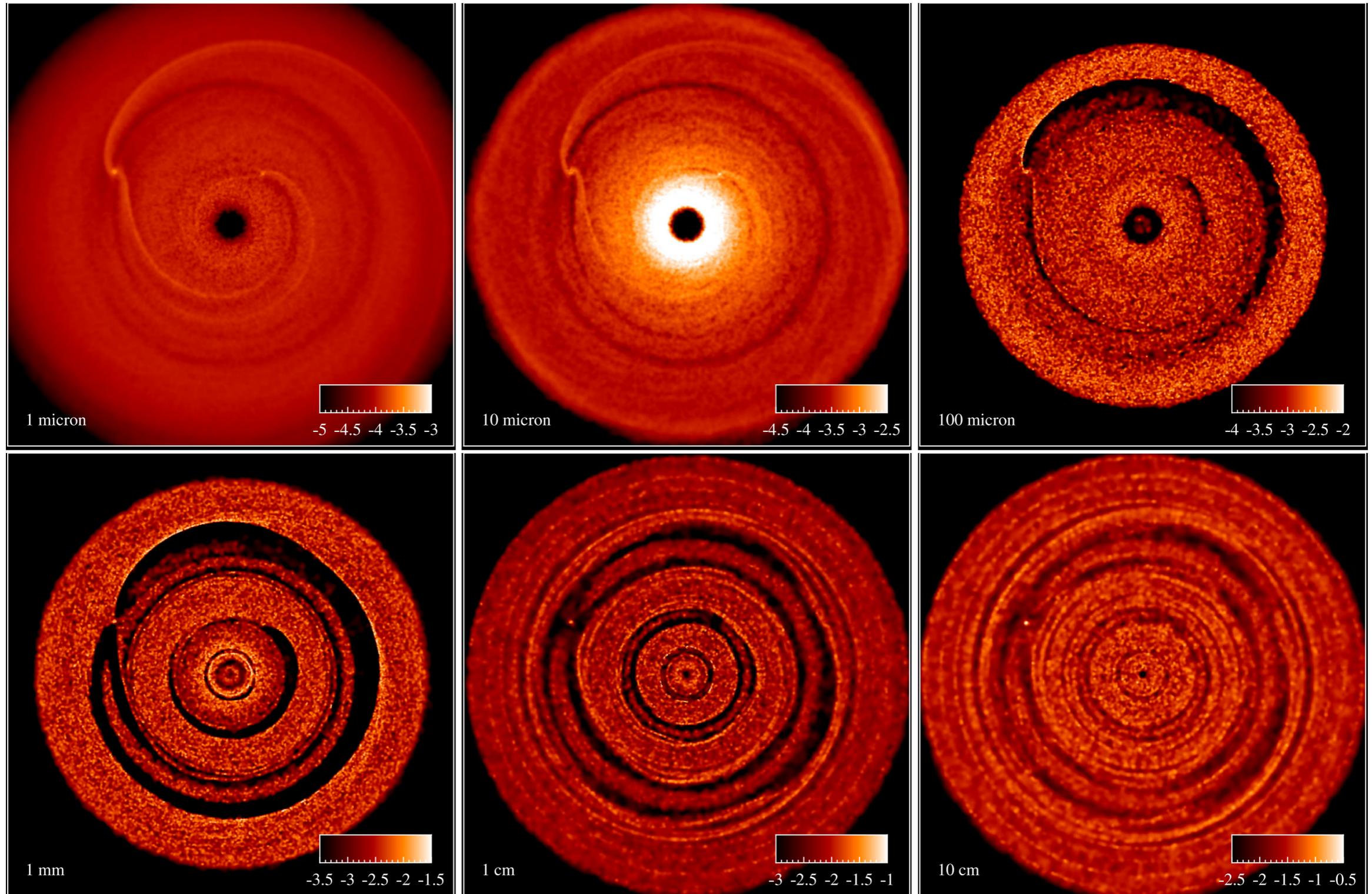
# DUST+GAS IN DISCS

# GAS VS DUST IN PROTOPLANETARY DISCS



# GAS VS DUST IN PROTOPLANETARY DISCS

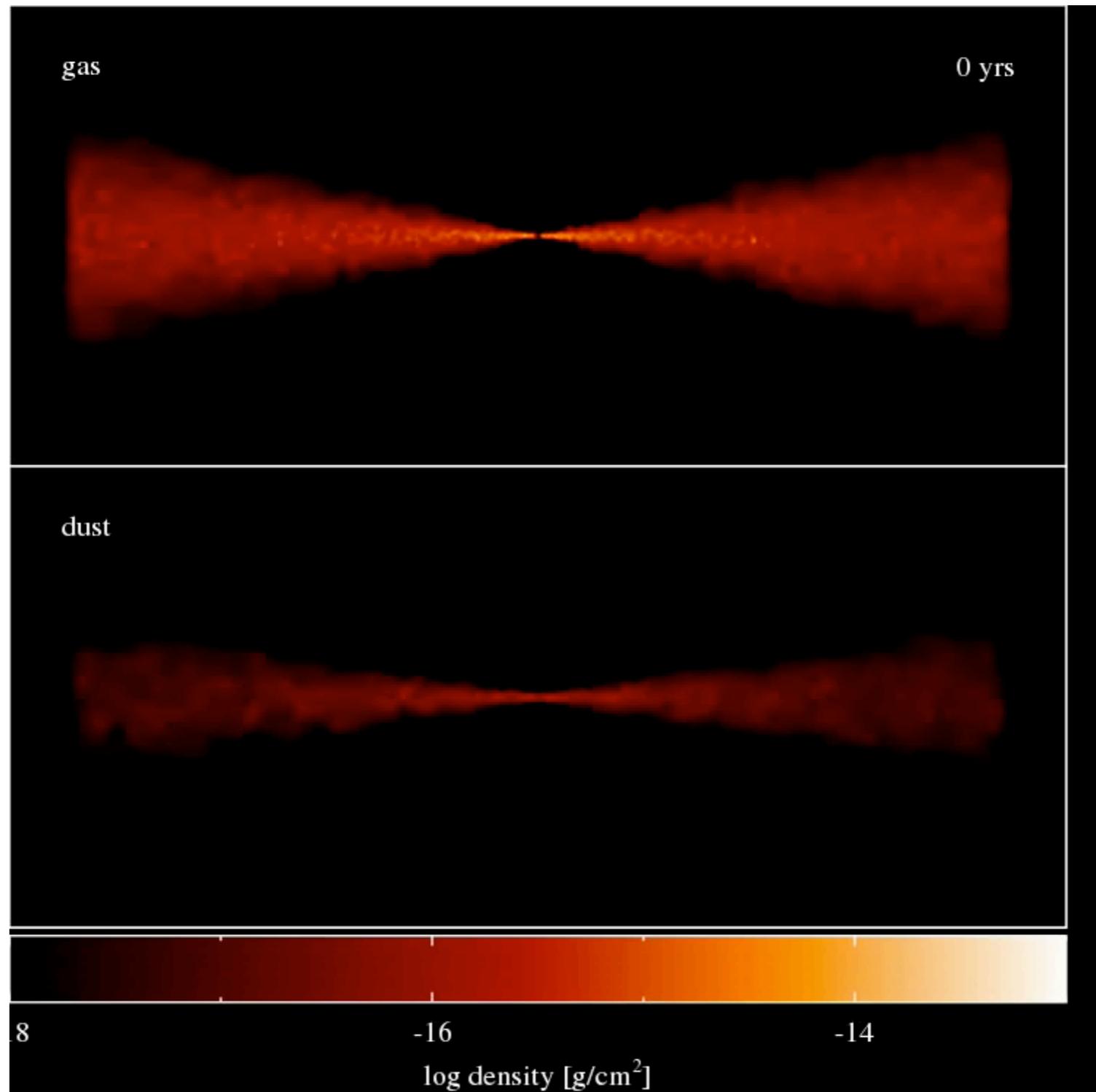
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*Dipierro et al. (2015)*

# GAS VS DUST IN PROTOPLANETARY DISCS

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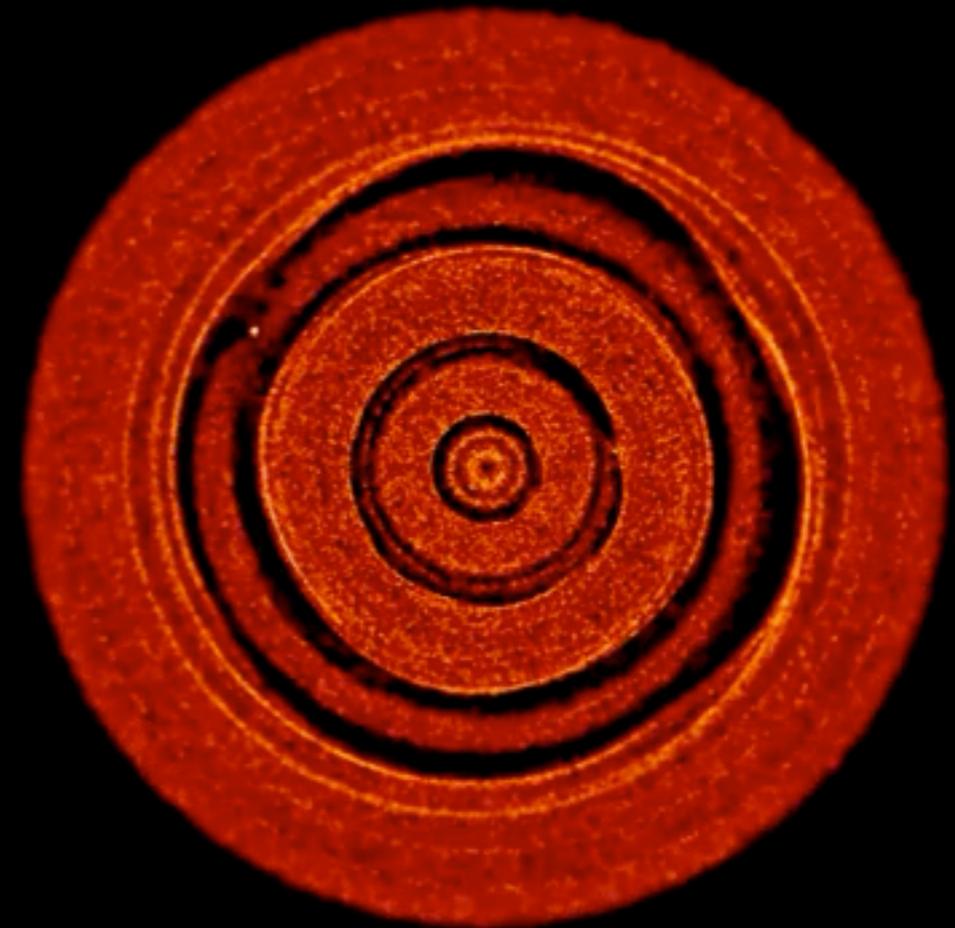
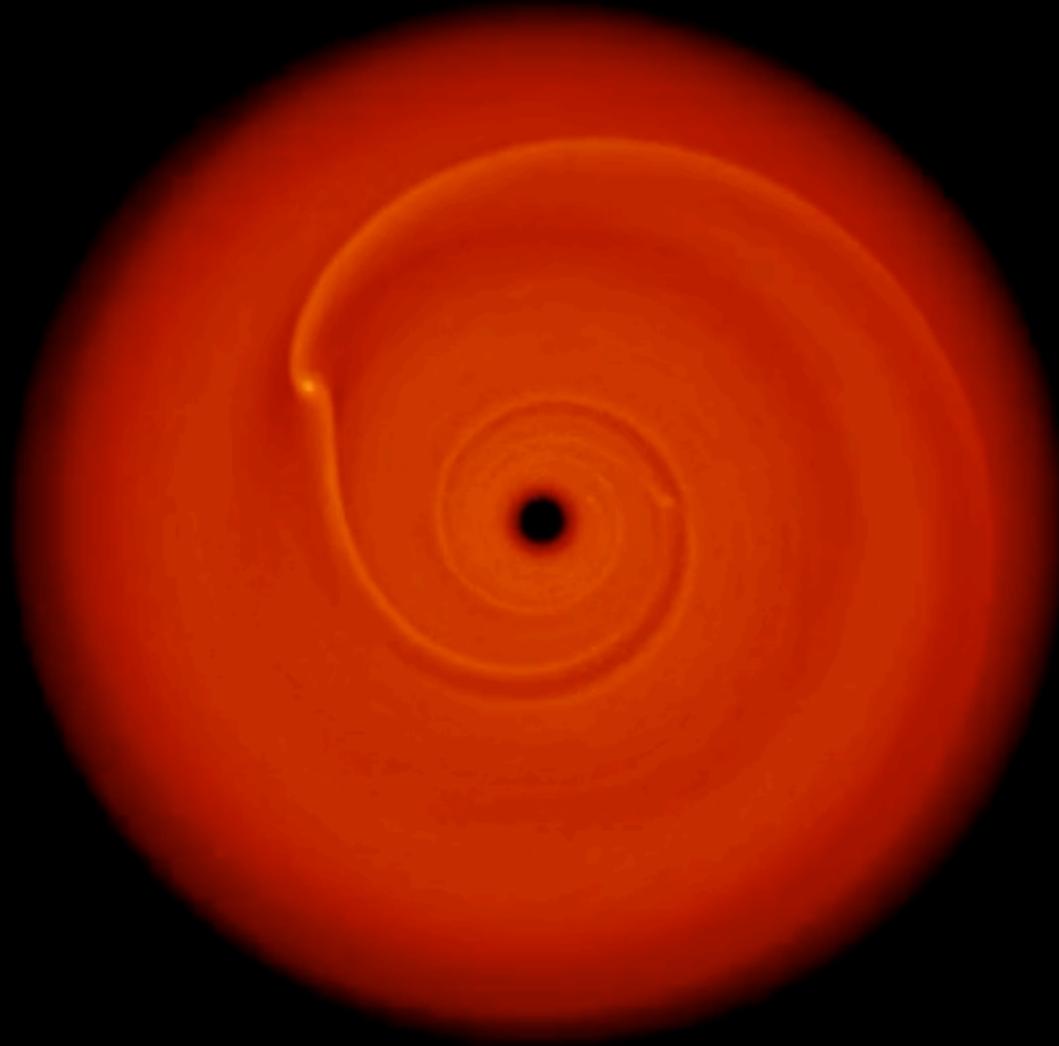
# GAP CARVING: GAS VS DUST

Require 3 approximately Saturn mass planets

gas

dust

3706 yrs



Dipierro, Price, Laibe, Hirsh, Cerioli and Lodato

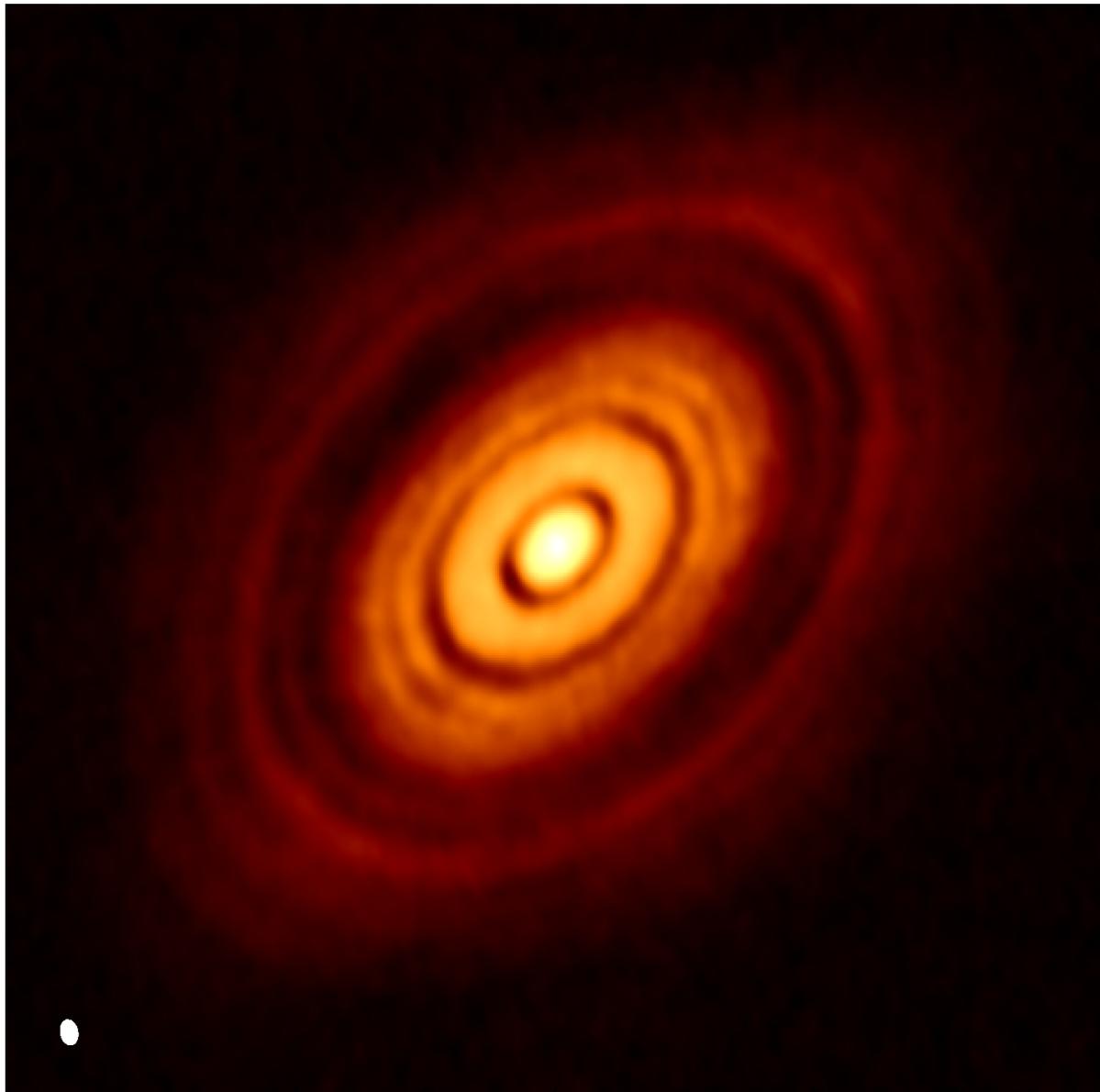
No gas gap, but sharp rings in dust!

*Dipierro et al. (2015)*

# HL TAU: OBSERVATIONS MEET THEORY

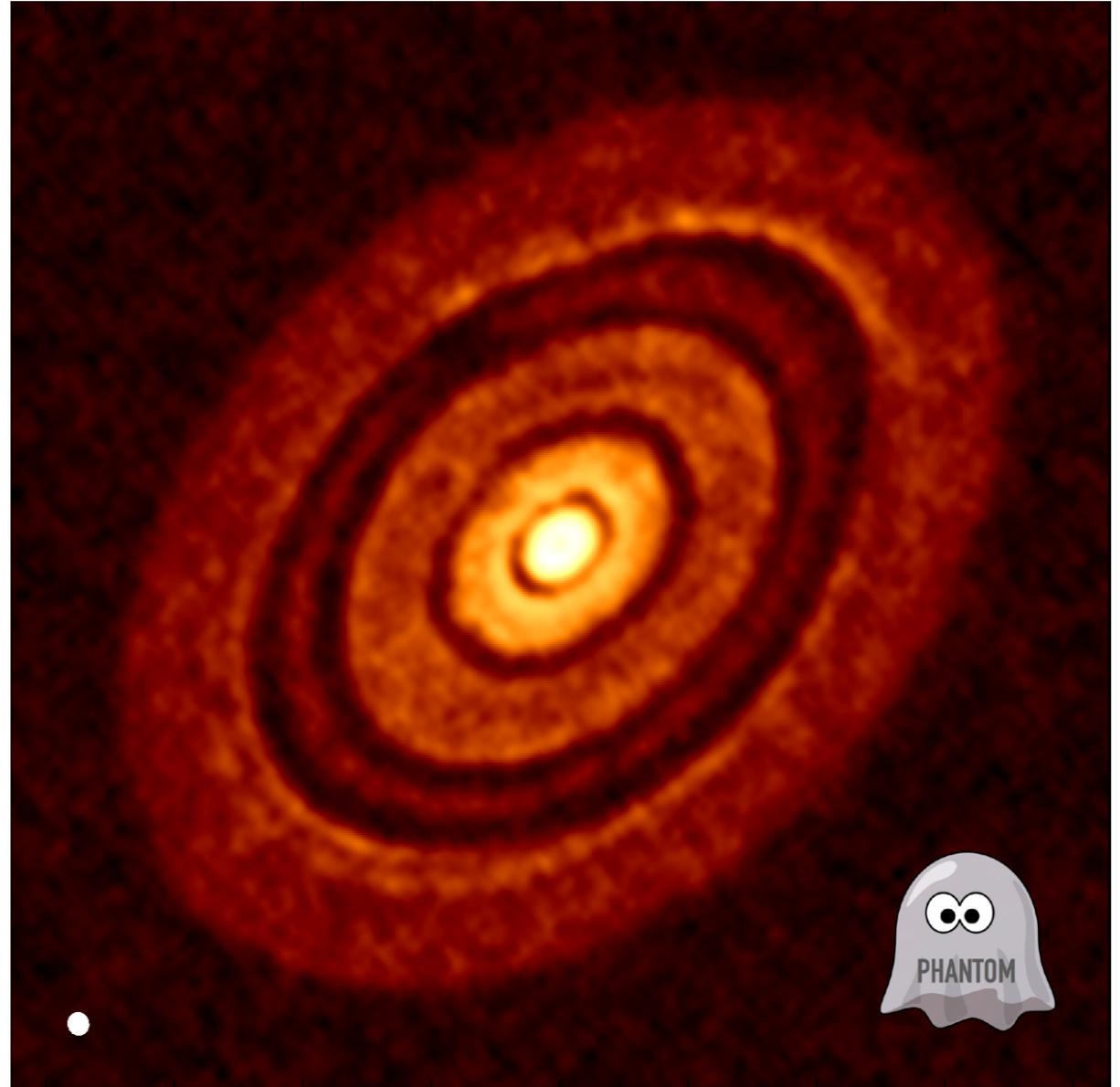
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Computed using RADMC3D  
radiative transfer (Dullemond  
2012) plus ALMA simulator



*Observed image*

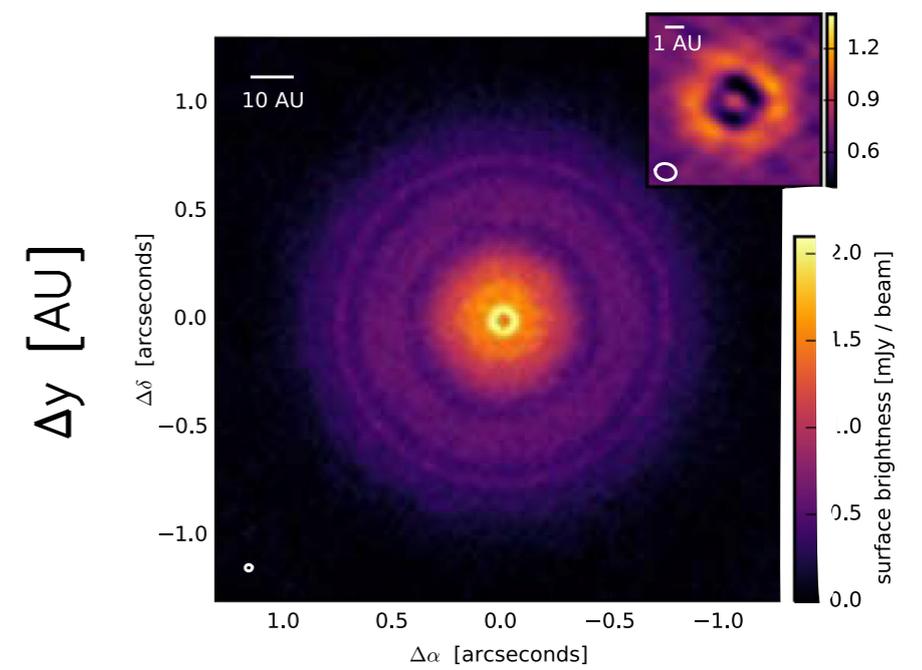
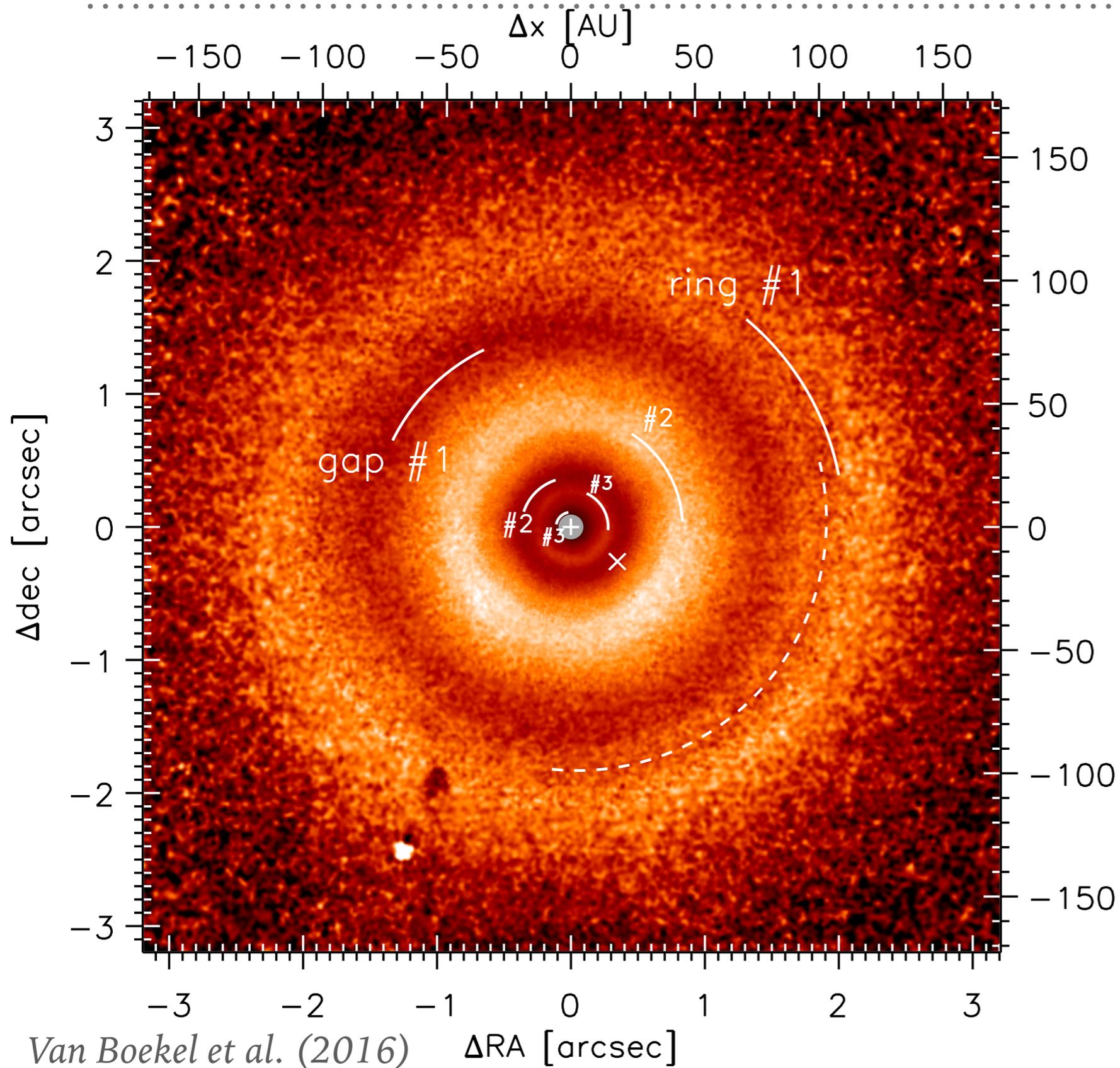
Credit: ALMA partnership et al. (2015)



*Our simulation*

Dipierro, Price, Laibe, Hirsh, Cerioli & Lodato (2015)

# TW HYA: GAS VS DUST

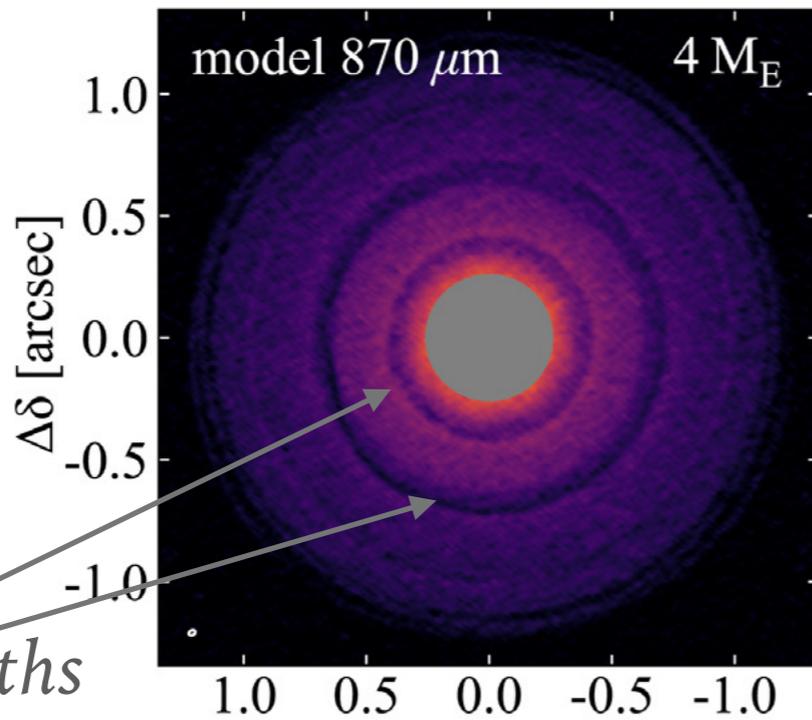


*Andrews et al. (2016)*

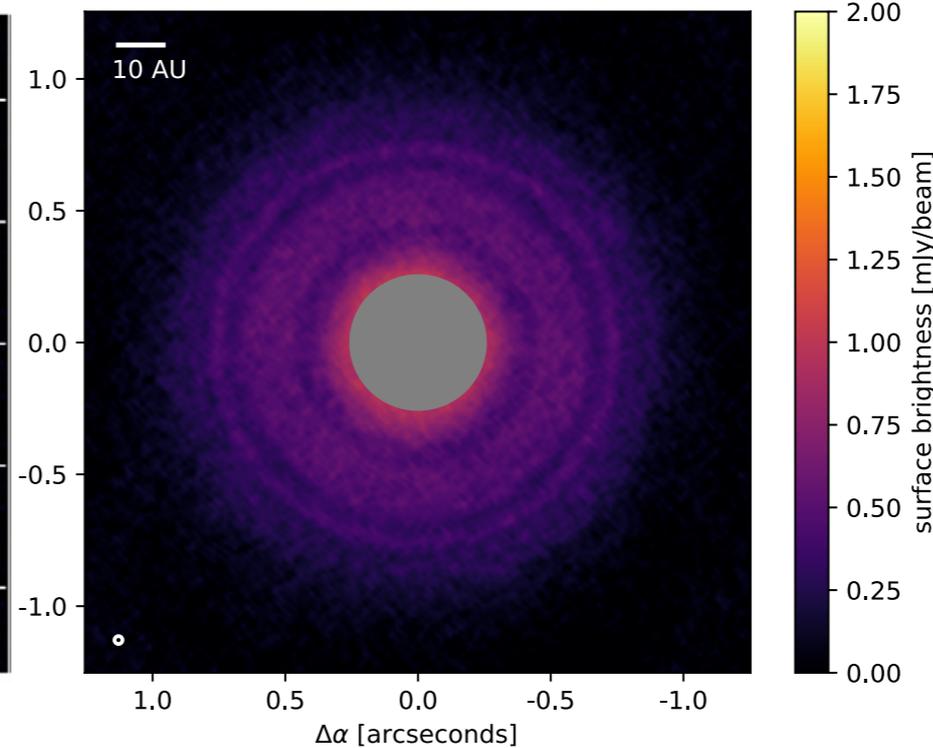
# TW HYA: MODELS VS OBSERVATIONS

*Mentiplay, Price & Pinte (2019)*

*Super-earths in TW Hya*

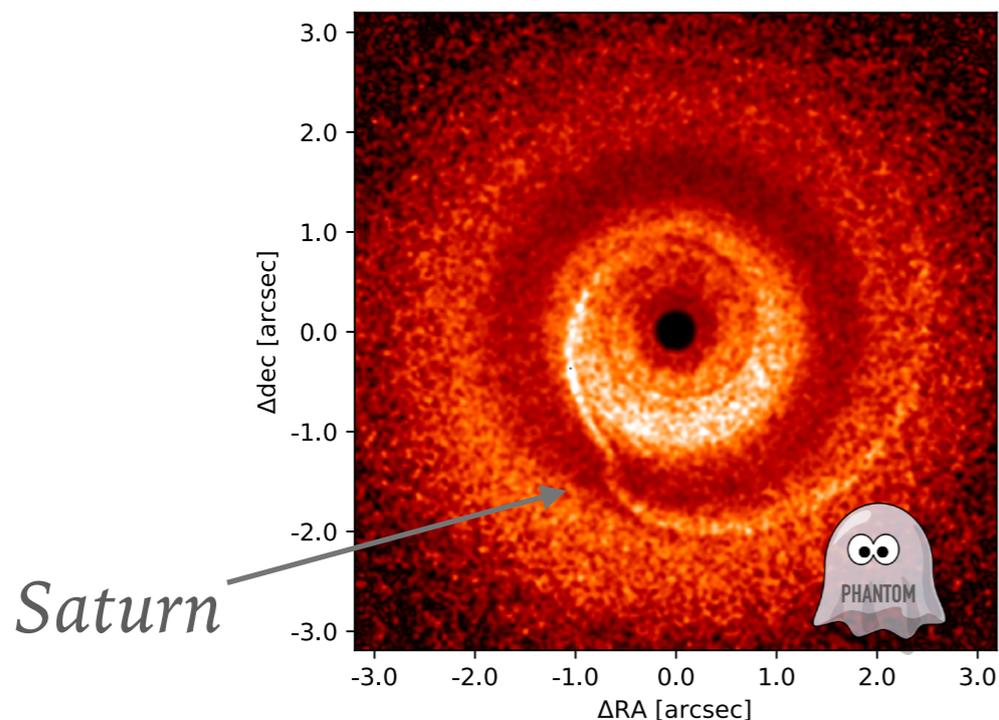


*Super Earths*

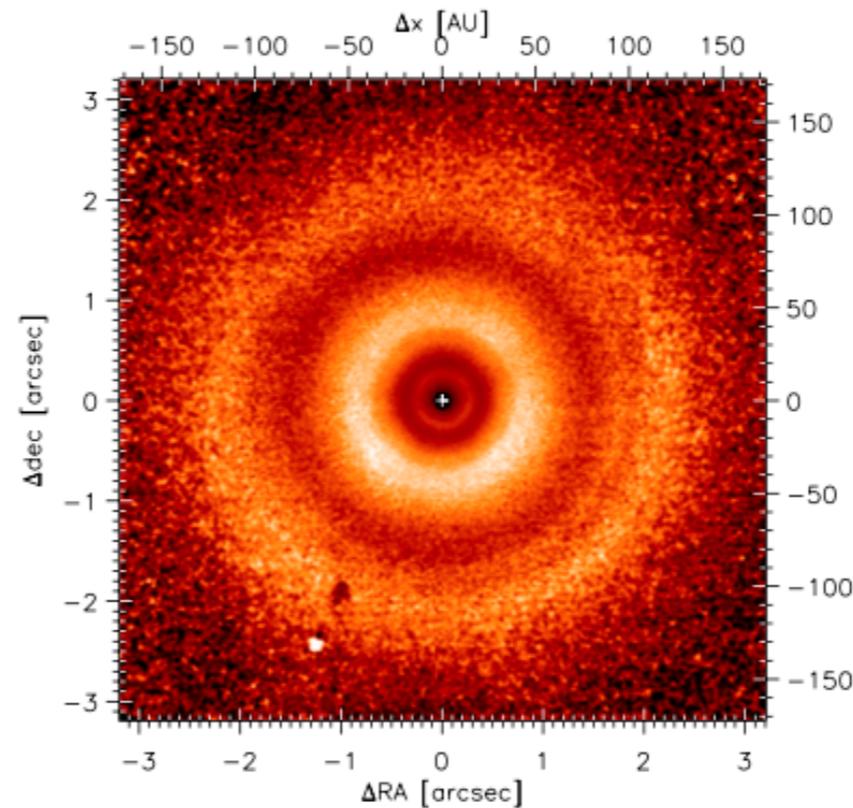


*Left: Our simulation*

*Right: Andrews et al. (2016)*



*Saturn*

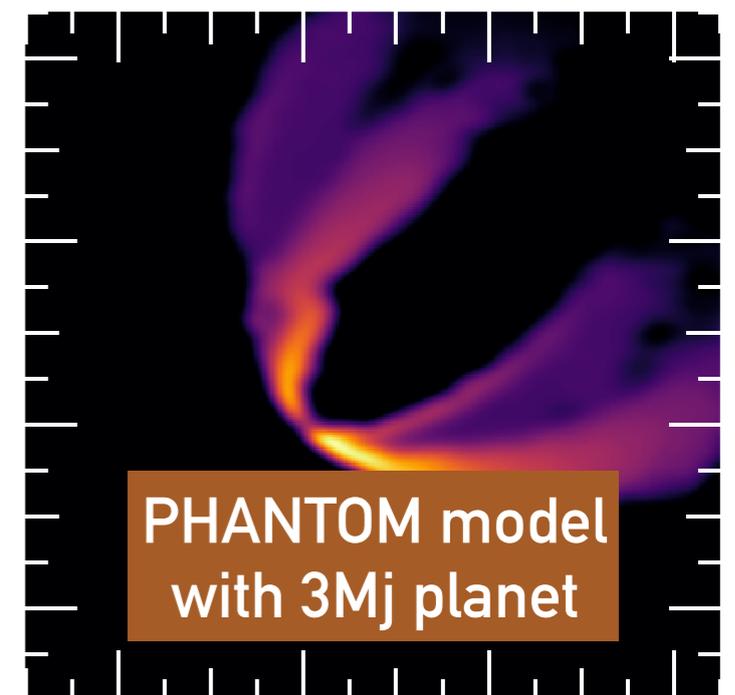
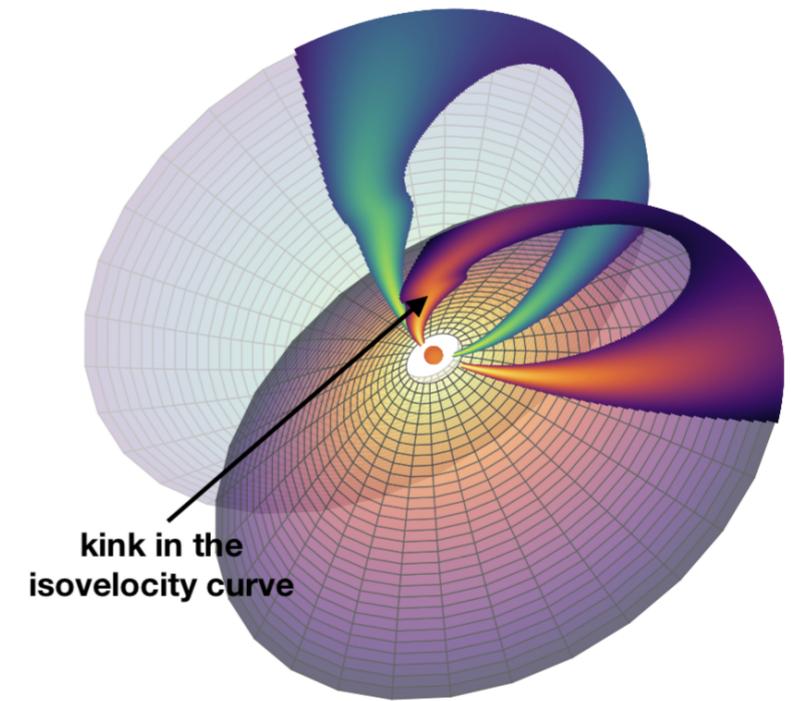
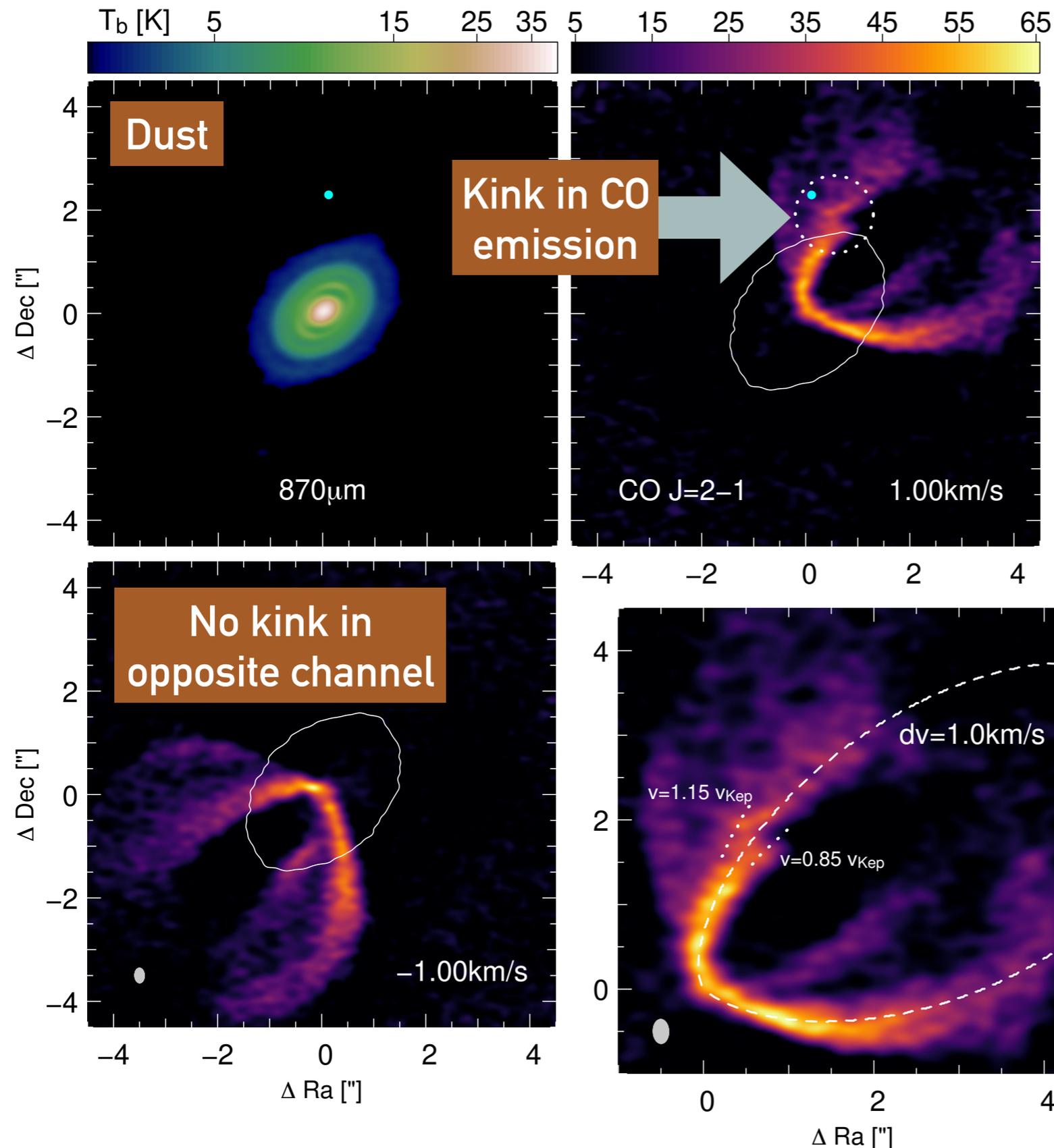


*Left: Our simulation*

*Right: Van Boekel et al. (2016)*

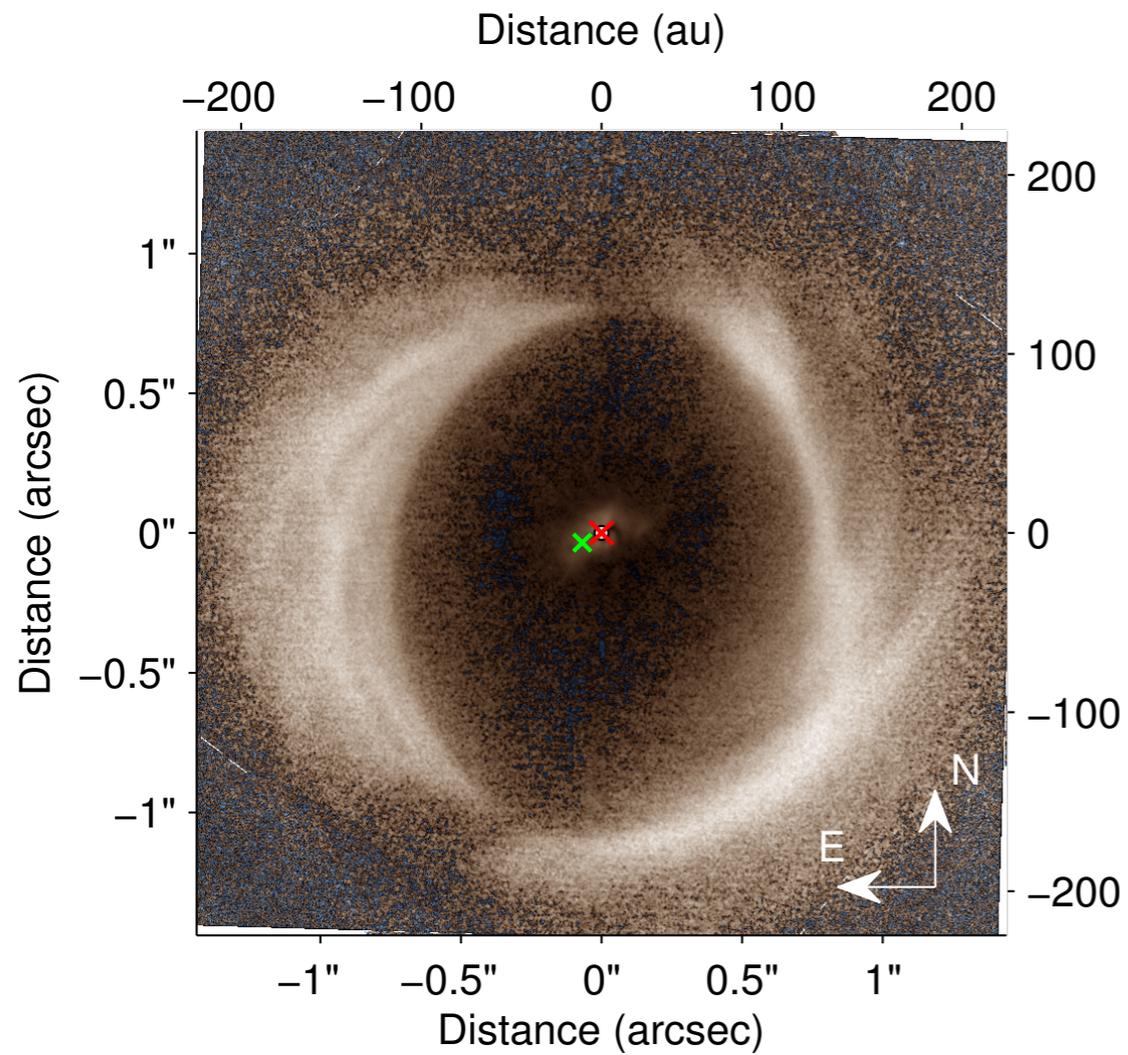
# KINEMATIC DETECTION OF A PROTOPLANET

*Pinte et al. (2018)*

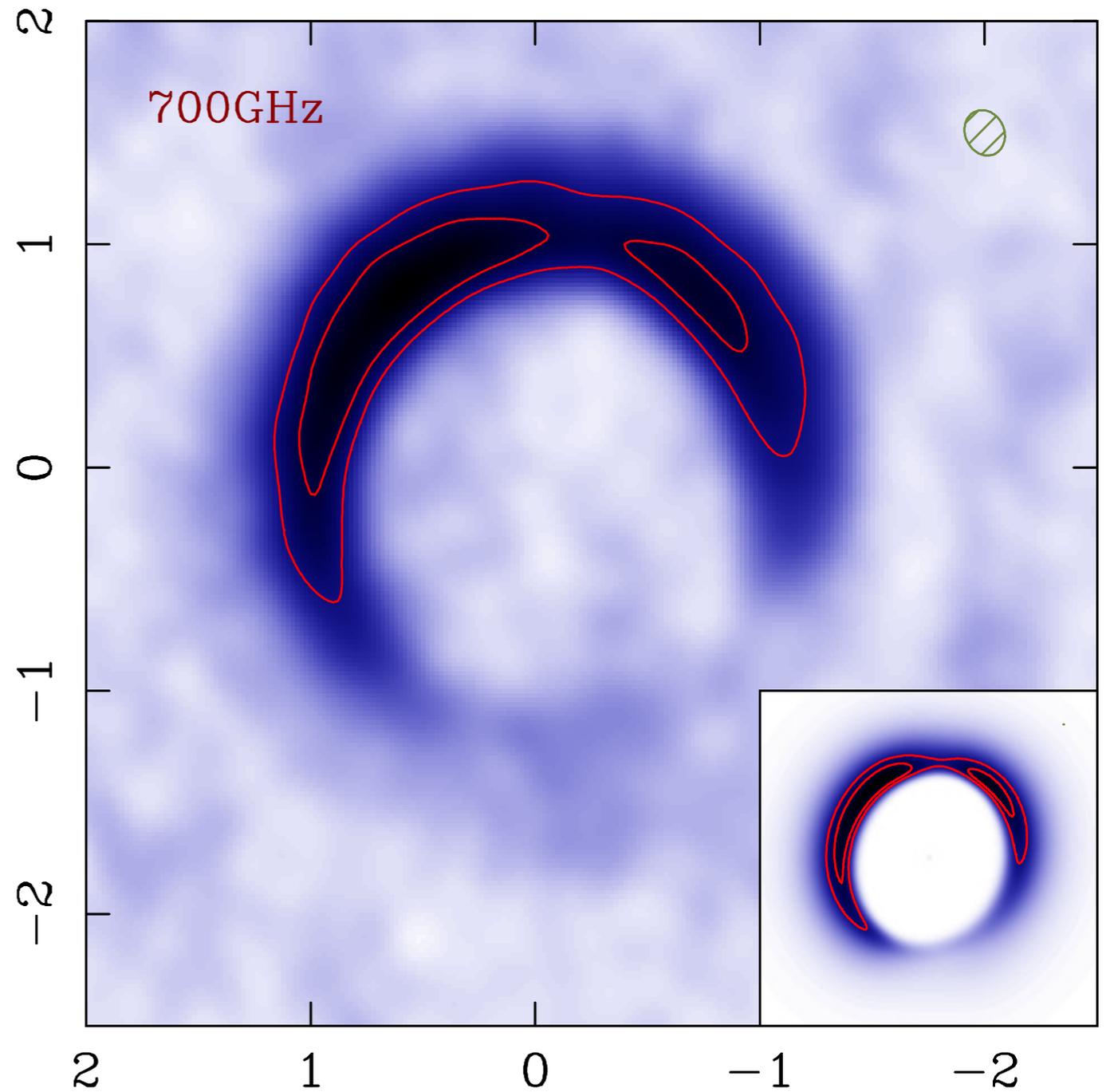


# HD142527: GAS VS DUST

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*Avenhaus + (2017)*



*Casassus + (2015)*

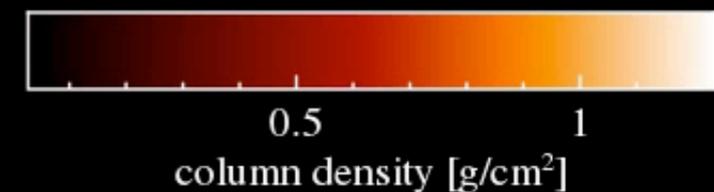
# DISC-BINARY INTERACTION IN HD142527

*Price et al. (2018)*

t=3176 yrs

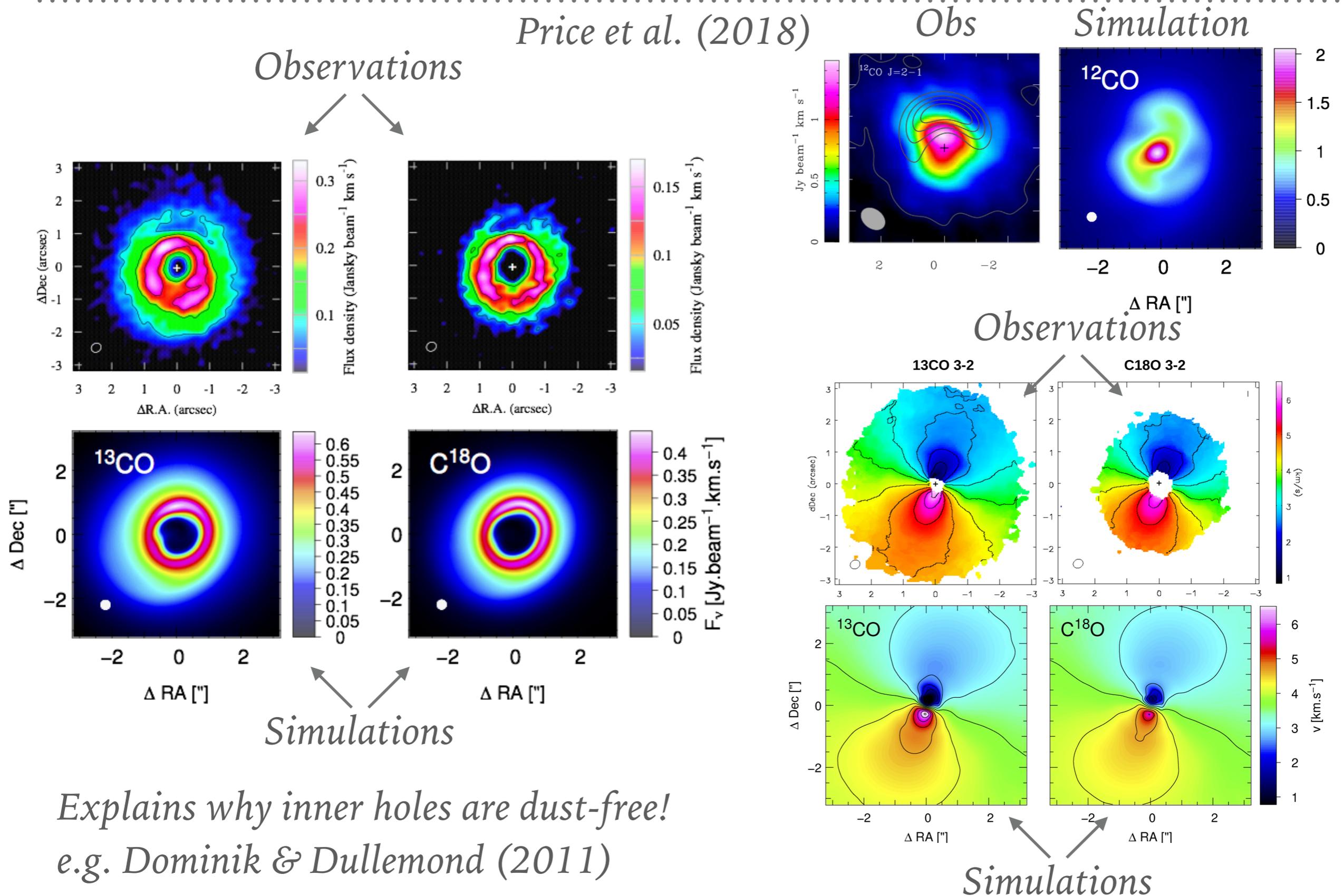


100 au

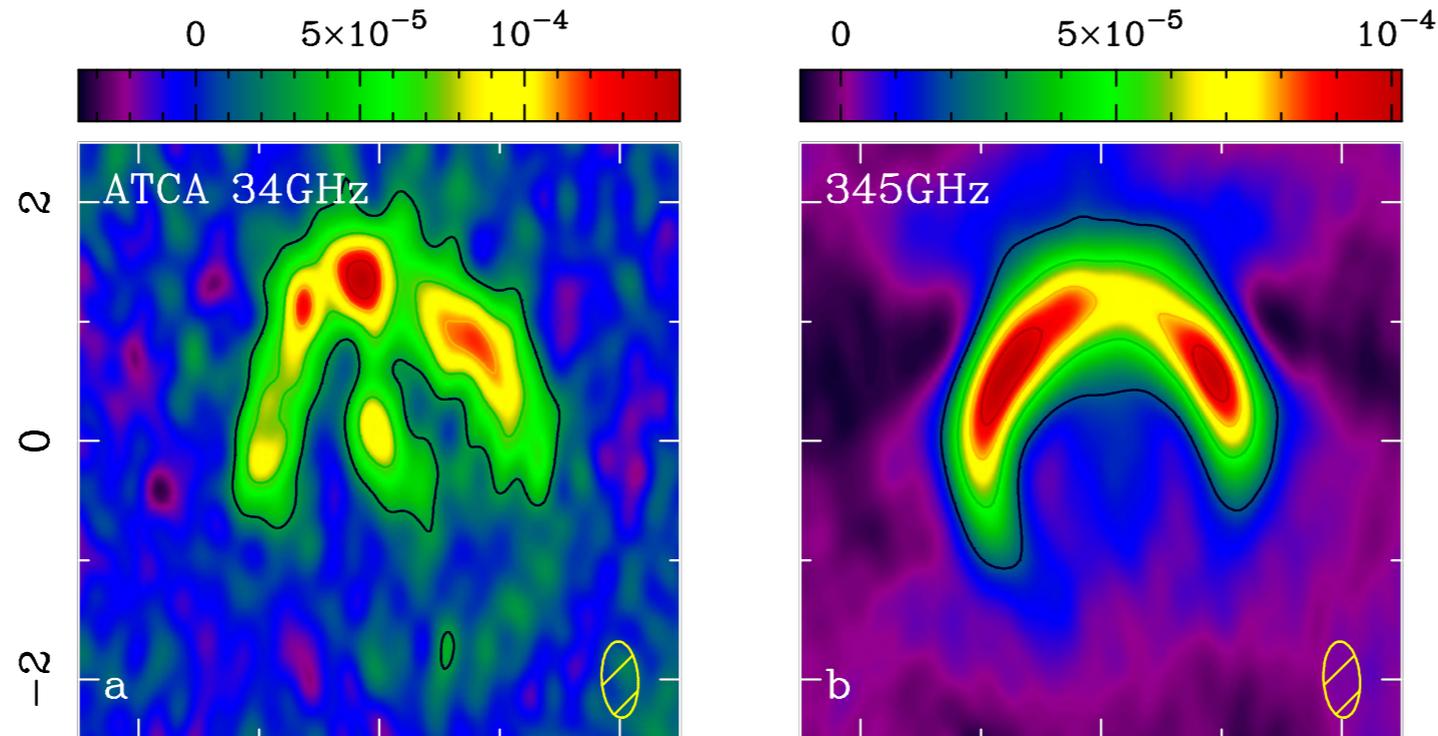


*See almost polar alignment of binary to disc, c.f. Aly et al. (2015), Martin & Lubow (2017)*

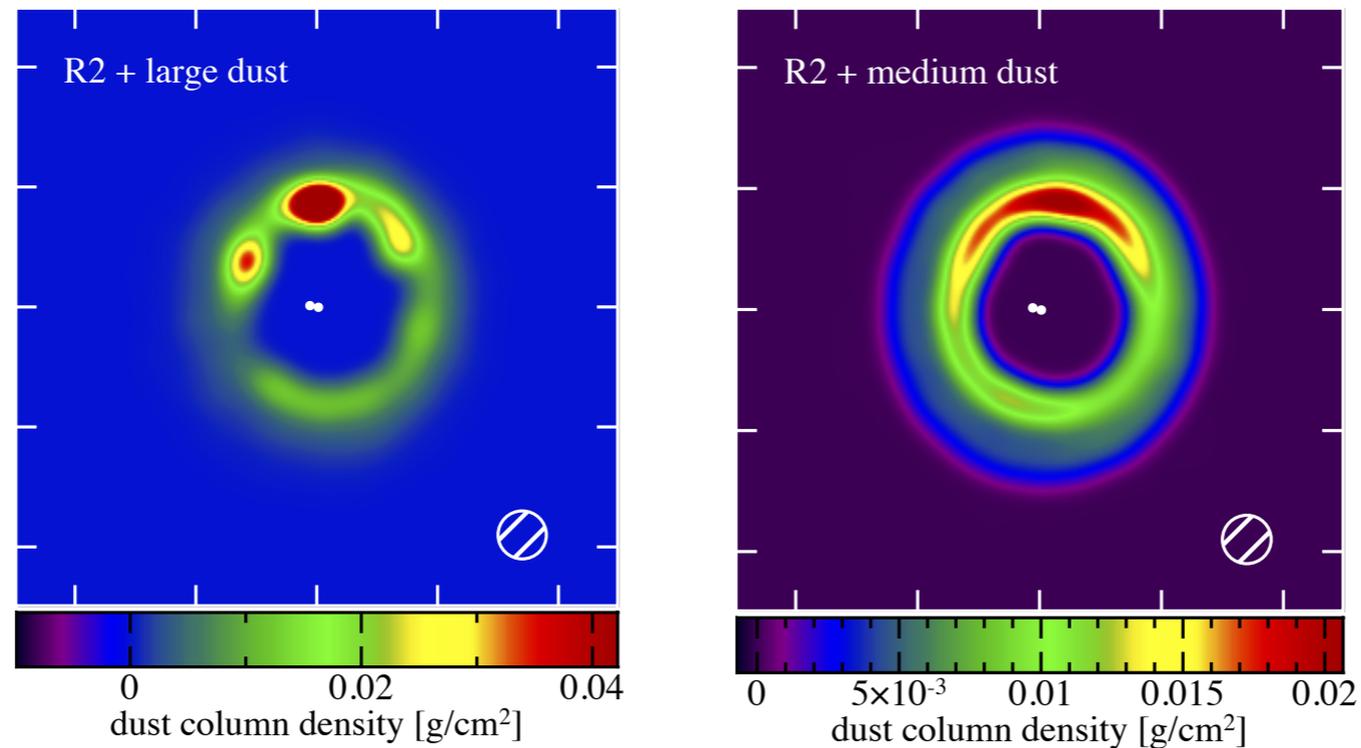
# OBSERVATIONS VS MODELS USING MCFOST (PINTE+2006)



# DUST HORSESHOE: OBSERVATION VS MODELS



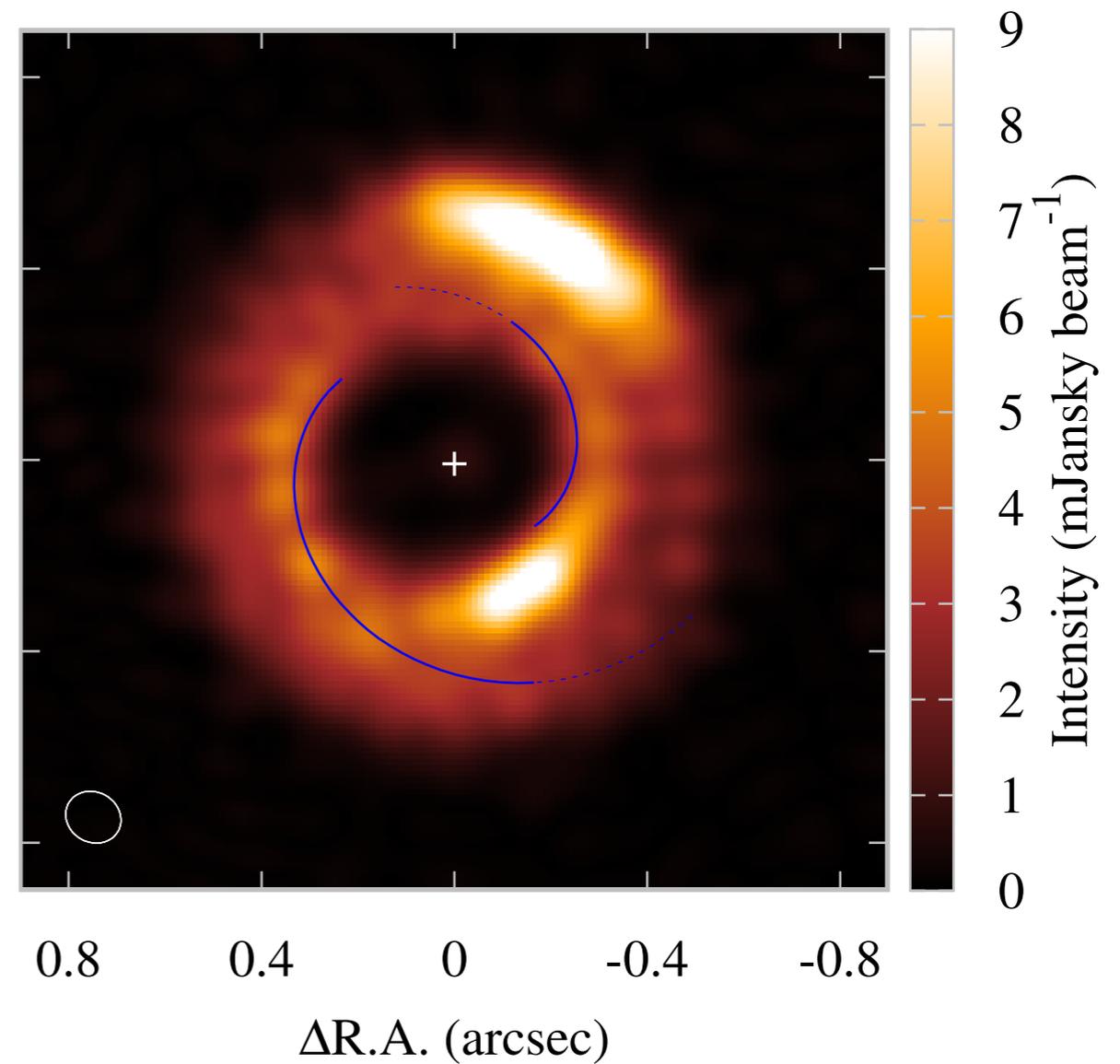
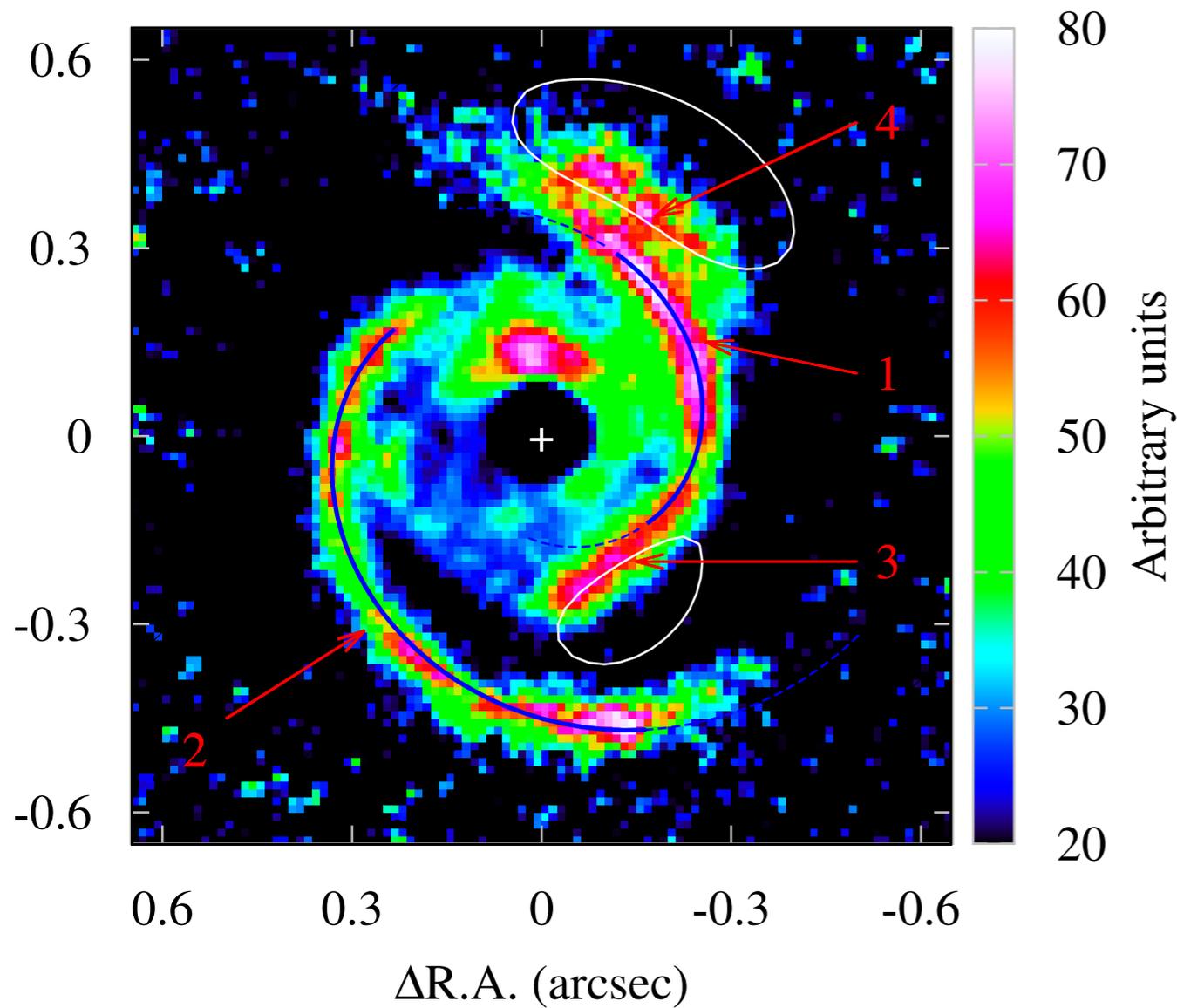
*Observations*  
*Casassus et al. (2015)*



*Simulations*  
*Price et al. (2018)*

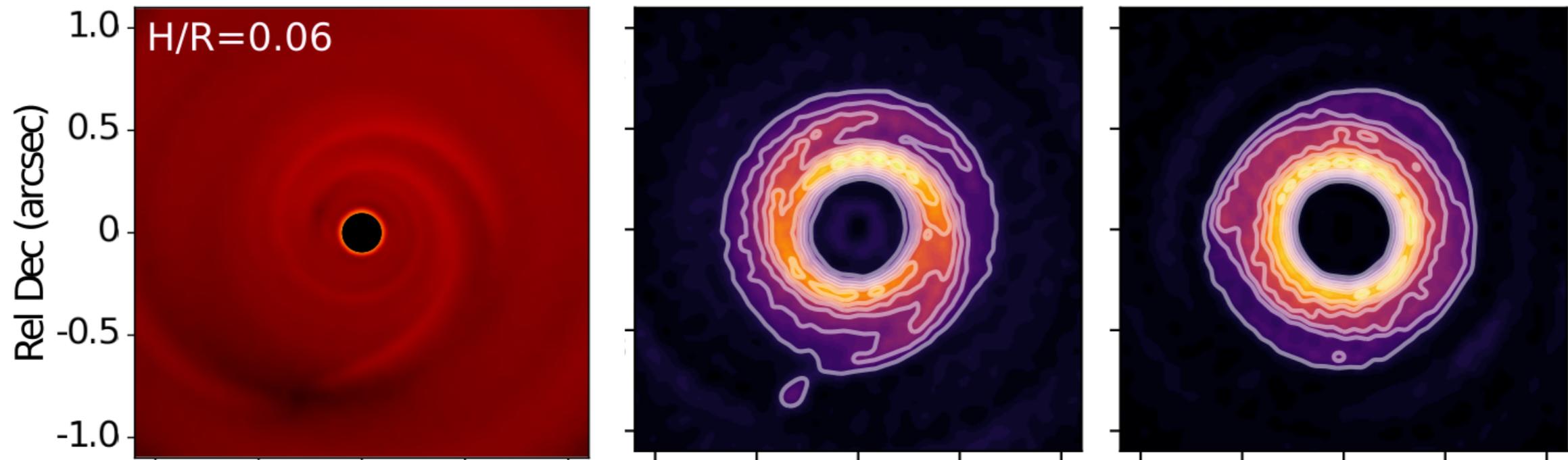
# MWC758: GAS VS DUST

*Boehler + (2018)*



# GAS VS DUST AROUND PLANET-CARVED CAVITY

Increasing Stokes number  $\longrightarrow$



Spirals become rings as Stokes number approaches unity

Can use as proxy for the gas disc mass

*Explains morphology difference in MWC758*

*Veronesi+2019, submitted*

# CONCLUSIONS

# THE COSMIC DUST (R)EVOLUTION

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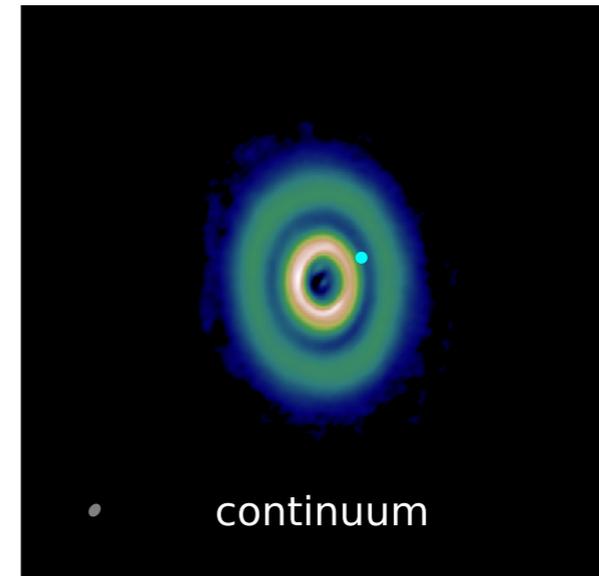
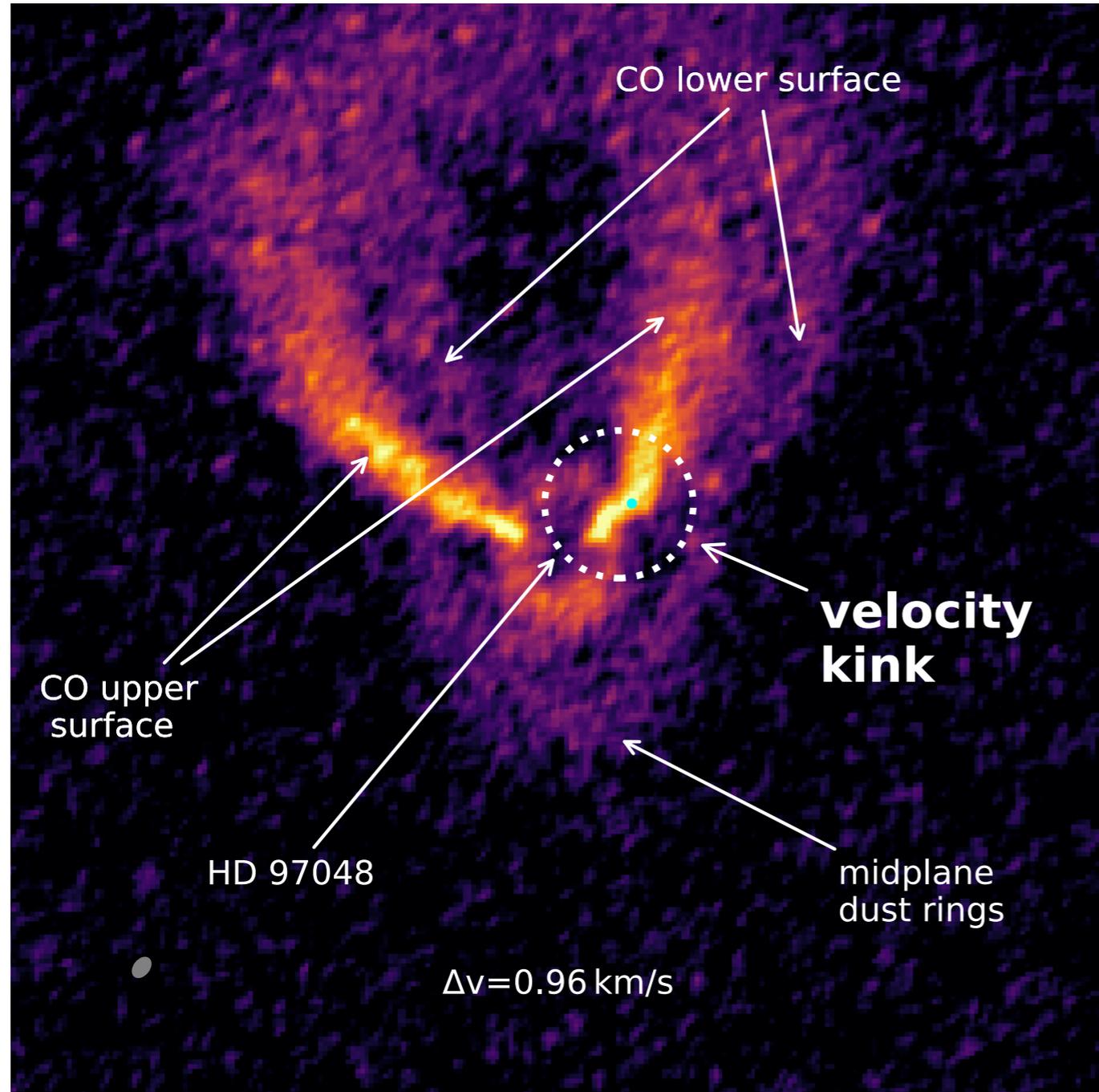
- Gas and dust already start to decouple in the ISM
- Dust and gas are DECOUPLED in protoplanetary discs  
- doing completely different things
- Planet formation is well underway (maybe even finished) by the time we observe protoplanetary discs



*PS: Thanks to the EU for funding the  
Dustbusters RISE network!*

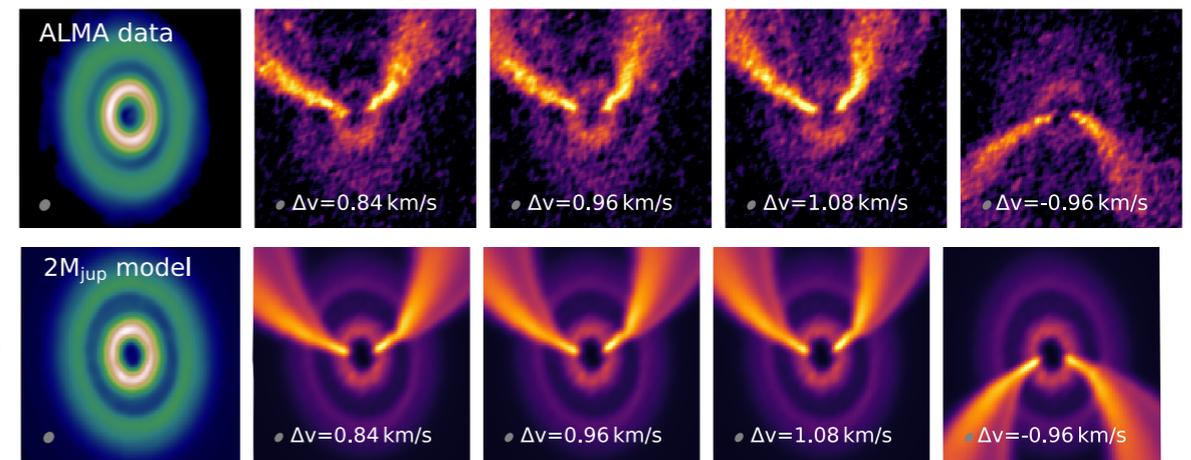
# SECOND ALMA PROTOPLANET DETECTION!!

*Pinte et al. (2019)*



Pinte et al. (2019)

[howmanyplanetshaschristophefound.com](http://howmanyplanetshaschristophefound.com)



2-3 MJup PLANET CARVING A GAP AT 130AU!